## The Stock Market

The safe way to double your money is to fold it over once and put it in your pocket.

Frank Hubbard, Journalist

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What do you think Frank Hubbard meant in this quote?

In the future, you will incur many expenses, such as a home, automobile, insurance, food, clothing, and health care. Some are major expenses and some are minor, but each costs money. To have money for major expenses, it helps to have your savings grow in value. Investing can help money grow in value.

You need to find a personal balance between risk and reward when you make choices about investments. Investments are never without questions. Did you miss the chance to make more money because you were being overly cautious? Was the investment too risky? Did you risk losing too much money by investing in something that may not have had a sound foundation?

Investors struggle with these questions every day. The stock market is a forum in which the investment risk/reward balance is put to the test. Will the market advance? Will the market decline? No one can be certain. With a strong knowledge of the stock market, you as an investor can make decisions that are based on experience, data, trends, and mathematics.

C orporations sometimes choose names that are personal, humorous, historical, or psychological. Below are some wellknown corporations and how their names were established.

AMAZON.com was originally known as Cadabra.com. The name was changed by its founder Jeff Bezos. He selected Amazon as a corporate name because the Amazon River is known as the biggest volume river in the world. He also wanted a name that began with A so that alphabetically it would appear at the top of a list of similar corporations.

COCA-COLA is a name that has its origins in the flavoring used to make the product - coca leaves and kola nuts. The founder, John Pemberton, changed the " $K$ " in kola to a "C" for appearance purposes.

ADIDAS is taken from the name of the company's founder Adolph (Adi) Dassler.
eBay was created by Pierre Omidyar, who originally wanted to use the name Echo Bay. The name was already taken by a gold mining company, so he shortened it to eBay.

XEROX comes from a Greek expression for "dry writing." The Xerox process was invented in 1937 by law student Chester Carlson.


## Objectives

- Learn the basic vocabulary of business organizations.
- Compute financial responsibility of business ownership based on ratios and percents.


## Key Terms

- capital
- corporation
- sole proprietorship
- profit
- personally liable
- shares of stock
- shareholders
- limited liability
- partnership


## How do businesses start?

Think of everything you use on a daily basis, from complex electronic devices to simple items like straws, paper clips, and toothbrushes. Have you ever wondered who invented them, or how each has been improved upon? Some inventions provide an opportunity to build a business, but not all. It takes imagination, money, and effort to create a successful business. The money used to start or expand a business is capitall.

A business owned by one person is a sole proprietorship. The owner, or proprietor, can hire people to help run the business, but these employees are not owners. The owner is responsible for all expenses, including labor and raw materials used in manufacturing a product or providing a service. The money left after all expenses are paid is profitt. The owner of a sole proprietorship is entitled to all of the profits. However, the owner is responsible, or personally liable, for any losses. Even if the business does not make a profit, the owner must still pay all of the bills of the business.

A business that is owned by a group of people, called partners, is a partmership. Partners share the profits and the responsibility for any losses. The partners are personally liable for any losses. Personal liability may require risking personal property. Sole proprietors and partners must consider this possibility when creating a business.

A corporation is a business organization that can be owned by one person or a group of people. Each owner who invests money in the corporation receives slhares of stock in the corporation. The owners are called sharelholders. Stock certificates are used as proof of ownership. Unlike sole proprietorships and partnerships, the shareholders in a corporation have limited liabillity-each owner cannot lose more than the value of his or her share of the business. The number of shareholders in a corporation depends on the structure of the business. When anyone can purchase stock in a corporation, the corporation is a pulblic corporation. You might already be familiar with public corporations, such as NIKE, McDonald's, Xerox, and Apple. The prices of shares of stock in public corporations can be found in newspapers, on television business channels, and on the Internet.

## Skills and Strategies

When a business is owned by more than one person, the owners do not necessarily own equivalent portions of the business. Ratios and percents can be used to represent the financial responsibility of owners and partners. Recall the relationship between decimals and percents.

To convert a decimal to a percent, multiply the decimal by 100.
To convert a percent to a decimal, divide the percent by 100.

## EXAMPLE 1

- Michelle invests $\$ 15,000$ in a partnership that has four other partners. - The total investment of all partners is $\$ 240,000$. What percent of the business does Michelle own?
: SOLUTION Represent Michelle's investment as a fraction of the total investment. Convert the fraction to a decimal and write as a percent.

Write as a fraction.

$$
\frac{\text { Michelle's investment }}{\text { Total investment }}=\frac{15,000}{240,000}
$$

Divide.

$$
\begin{aligned}
15,000 \div 240,000 & =0.0625 \\
0.0625 \times 100 & =6.25 \%
\end{aligned}
$$

Multiply by 100. Write a percent sign.
Michelle owns $6.25 \%$ of the partnership.

## CHECK YOUR UNDERSTANDING

Kyle invests \$20,000 in a partnership that has five other partners.
The total investment of the partners is $\$ 160,000$. What percent of the business is owned by the five other partners?

## EXAMPLE 2

- The total number of shares of stock in the Bulls Corporation is 650,000 . Mike owns $12 \%$ of the shares. How many shares of Bulls Corporation stock does he own?
SOLUTION Let $x$ represent the number of shares Mike owns.

$$
\begin{array}{lrl} 
& \text { Express } 12 \% \text { as a fraction. } & 12 \%
\end{array}=\frac{12}{100} 0
$$

Mike owns 78,000 shares of Bulls Corporation.

## CHECK YOUR UNDERSTANDING

Jillian owns $60 \%$ of the stock in a private catering corporation. There are 1,200 shares in the entire corporation. How many shares does Jillian own?

## EXAMPLE 3

- Three partners are investing a total of \$900,000 to open a garden and landscaping store. Their investments are in the ratio 2:3:5. How much does the partner that invested the least contribute? SOLUTION Use the ratio 2:3:5 to write an expression for the amount each partner invested.

Let $2 x$ represent the amount invested by the first partner.
Let $3 x$ represent the amount invested by the second partner.

Let $5 x$ represent the amount invested by the third partner.

Write an equation showing the three investments total $\$ 900,000$.

$$
2 x+3 x+5 x=900,000
$$

Combine like terms. $\quad 10 x=900,000$
Divide each side of the equation by $10 . \quad x=90,000$
: The partner that invested the least is represented by the expression $2 x$.
: Substitute $\$ 90,000$ into the expression. $\quad 2(90,000)=180,000$
: The partner who invested the least amount contributed $\$ 180,000$.

## CHECK YOUR UNDERSTANDING

Two partners are starting a wedding planning business. The total investment is $\$ 45,000$. Their investments are in the ratio $4: 5$. How much does each investor contribute?

## EXTEND YOUR UNDERSTANDING

Two partners each invest $35 \%$ in a startup business. They need to find another investor for the rest of the money. What percent of the business will that person own? Write a ratio to represent the investments in the business.


Genius is $1 \%$ inspiration and 99\% perspiration. Accordingly a
genius is often merely a talented person who has done all of his
or her homework.
Thomas Edison, Inventor

1. What do you think Thomas Edison meant by the word perspiration? How do those words apply to what you've learned in this lesson?
2. Tomika owns $\frac{3}{5}$ of a law partnership. What percent of the partnership does she own?
3. Ryan owns three-eighths of a florist shop worth $\$ 76,000$. What is the value of Ryan's share of the business?
4. A corporation issues $1,200,000$ shares of stock at its beginning to shareholders. How many shares must a shareholder own to have a majority of the shares?
5. Elisa owns $28 \%$ of the Grudman Corporation. The rest of the shares are owned equally by the remaining six shareholders. What percent of the corporation does each of the other shareholders own?
6. Julie and Kristen are the partners in a local sporting goods shop. They needed $\$ 51,000$ to start the business. They invested in the ratio $5: 12$, respectively.
a. How much money did each invest?
b. What percent of the business was owned by Kristin? Round to the nearest tenth of a percent.
c. If the business grows to $\$ 3,000,000$, what percent of it will Julie own? Round to the nearest tenth of a percent.
7. Joe, Thea, and Taylor invested in a partnership in the ratio 1:4:7, respectively. Years later, when the partnership was worth $\$ 1.6$ million, Thea decides to go to graduate school and sells her part of the partnership to Joe.
a. How much would Joe need to pay Thea to buy her share of the business? Round to the nearest dollar.
b. What percent of the business will Joe own after he buys Thea's portion? Round to the nearest tenth of a percent.
8. Seventy-two percent of the shareholders in a service corporation are women. If the corporation is owned by 45,600 people, how many of the shareholders are women?
9. The 120 shareholders of a corporation are voting for a new Board of Directors. Shareholders receive one vote for each share they own. Would it be possible for one shareholder's votes to choose the new Board of Directors? Explain.
10. The top $x$ shareholders in a corporation each own $y$ shares of a certain stock. The corporation's ownership is represented by a total of $w$ shares of stock. Express the percent of the corporation owned by the top $x$ shareholders.
11. A corporation is having a shareholders meeting. Not all shareholders are able to attend. In fact, most usually do not. The ownership of the corporation is represented by $2,351,000$ shares of stock owned by 111,273 shareholders.
a. Must all of the shareholders own more than one share of stock?
b. If 3,411 shareholders attend the meeting, what percent of the shareholders are represented? Round to the nearest percent.
c. If the shareholders who do attend own a combined 1.8 million shares of the corporation, what percent of the shares are represented at the meeting? Round to the nearest percent.
12. A private corporation owned by 35 shareholders is worth $\$ 1.7$ million. The corporation loses a lawsuit worth $\$ 3$ million. What is the value of any personal property of the shareholders that can be taken to pay the settlement? Explain.
13. A partnership owned equally by 13 partners is worth $\$ 1.3$ million. The partnership loses a lawsuit worth $\$ 3$ million. What is the value of any personal property each partner must forfeit to pay the settlement? Explain.
14. A sole proprietorship is worth $w$ dollars. The owner loses a lawsuit against him for $y$ dollars where $y$ is greater than $w$. Express algebraically the value of the personal property the owner must forfeit to pay the settlement.
15. Six equal partners own a local pizzeria. The partners have made a tremendous profit and bought many personal items such as cars, boats, new homes, and so on. In order to protect their personal possessions, they decide to incorporate the pizzeria, so that the six partners own shares in the corporation and have limited liability. The business is worth $\$ 675,000$. After an accident, the partners lose a lawsuit and have to pay $\$ 1.2$ million in damages. How much money will each partner personally lose to pay this lawsuit? Explain.
16. Three people invest in a business. The first two invest in the ratio $2: 3$, and the third person invests twice as much as the other two combined. The total invested is $\$ 30$ million.
a. How much did the major investor contribute?
b. Does the major investor own more than half the business?
c. What fraction of the business does the major investor own?
17. Ten years ago, Lisa bought a hair salon for $x$ dollars. She built up the business and it is now worth nine times what she paid for it. She decides to sell half of the business to a friend, and they become partners. Express the amount Lisa's friend must pay Lisa to buy half the business.
18. Four people invested in a restaurant. One person invested $\$ 100,000$. Two others invested in the ratio $x: 2 \mathrm{x}$, and the fourth person invested an amount equal to the other three investors combined.
The total investment was $\$ 1,100,000$.
a. Write an expression for the amount invested by the fourth person.
b. Write an equation that allows you to find the amount invested by each person.
c. How much did each person invest?

## Stock Market Data <br> 1-2

## Key Terms

- stock market
- high
- trades
- NYSE
- NASDAQ
- last
- close
- low
- volume
- Sales in 100 s
- 52-week high
- 52-week low
- net change
- after-hours trading
- spreadsheet
- cell


## Objectives

- Use stock data to follow the daily progress of a corporate stock.
- Write spreadsheet formulas.


## What Stock market data is available

## ON A DAILY BASIS?

Stock marlket is a general term for an institution through which stocks are bought and sold. Stock market transactions are known as trades. The two most well known stock markets are the New York Stock Exchange (NYSE) and the National Association of Securities Dealers Automated Quotation System (NASDAQ). A wise investor in stocks makes data-driven decisions by examining short and long term trends, changes, fluctuations, and consistencies. Investors intend to profit from their investments. You don't need to be a professional stockbroker or a financial analyst to follow the market. What you need is an understanding of trading data. This data can be found in newspapers, online, or on television financial channels. The best source for information is the Internet because it is current and accurate within minutes of a market event. However, you want to be certain that you are using a credible source.

In order to interpret stock market data, you need to know the meaning of the categories used in stock market international charts.

- Last is the price per share of the last trade that was made for a particular stock. In a newspaper, the last amount is usually the closing price for the trading day. Online, it is usually the price of the last trade made for one share of the stock.
- Close or closing price is the last price at which a stock was traded during a regular day's trading session. For most stock markets across the country, the daily sessions run from 9:30 A.m. to 4:00 p.м. Eastern Standard Time.
- High is the highest price at which one share of the stock was traded on a given day.
- Low is the lowest price at which one share of the stock was traded on a given day.


| AT\&T 37.70 | 0.11(29\%) |
| :--- | ---: |
| as of 2:11 P.M. |  |
|  |  |
| Last Trade: | 37.59 |
| Trade Time: | $2: 03$ P.M. ET |
| Change: | $0.08(0.21 \%)$ |
| Prev Close: | 37.51 |
| Open: | 37.46 |
| Bid: | N/A |

- Volume is the number of shares that was traded in a given time period. In a newspaper, the volume is usually the day's volume. Online, the volume represents the total number of shares traded within a few minutes of the last trade. Sometimes the volume is listed as Salles in 100s. This represents the number of groups of 100 shares that were traded on a given day. Some websites may post the exact volume, while other websites state the volume in hundreds, thousands, or even millions.
- 52-week high is the highest price at which one share was traded over the last year.
- 52-week low is the lowest price at which one share was traded over the last year.
- Clig or net change shows the change between the previous day's closing price and the current day's closing price. This can be a monetary amount or it can be expressed as a percent. The change is positive if the current day's close is greater than the previous day's close and negative if the current day's close is less than the previous day's close.
- After-lhours tradling means that some trades are made after the market closes. A difference between one day's closing price and the next morning's opening price means after-hours trades on that stock occurred.


## Skills and Strategies

Examine the data for XYZ Corporation published at the close of two trading days. These categories are used when analyzing data about stock.

| XYZ Corporation | XYZ Corporation |  |  |
| :--- | :---: | :--- | :--- |
| May 5 |  | May 12 |  |
| Last | 52.20 | Last | 49.98 |
| Trade Time | $4: 00$ PM ET | Trade Time | $4: 00$ PM ET |
| Chg | 2.61 | Chg | -1.55 |
| Open | 50.10 | Open | 49.90 |
| 52-week High | 60.45 | 52-week High | 60.45 |
| 52-week Low | 43.60 | 52-week Low | 43.60 |
| Sales in 100s | 28000 | Sales in 100s | 32000 |
| High | 52.60 | High | 51.40 |
| Low | 49.00 | Low | 50.60 |

## EXAMPLE 1

What was the difference between the high and the low prices on May 5 ?
SOLUTION 1 The day's high price was $\$ 52.60$ and the low was $\$ 49.00$.
Subtract the low from the high. $\quad \$ 52.60-\$ 49.00=\$ 3.60$
The difference in the high and low prices on May 5 was $\$ 3.60$.

## CHECK YOUR UNDERSTANDING

What was the difference between the high and low prices on May 12 ?

## EXAMPLE 2

: On May 12, what was the actual volume of XYZ shares posted? Write the volume in thousands.
SOLUTION The data for May 12 does not use the category name volume. Sales in 100s indicates volume. Because volume in 100s is the number of groups of 100 shares traded, 32,000 hundreds is written

$$
32,000 \times 100, \text { or } 3,200,000
$$

Sales in 1,000 s represent the number of groups of 1,000 shares traded.
Divide by $1,000 . \quad 3,200,000 \div 1,000=3,200$
On May 12, there were 3,200 thousands of shares traded.

## CHECK YOUR UNDERSTANDING

On May 5, what was the actual volume of XYZ shares posted? Write the volume in thousands.

## EXAMPLE 3

- At what price did XYZ Corporation close on May 4?

SOLUTION XYZ Corporation ended the trading day on May 5 with a closing price of $\$ 52.20$. This reflected a change of $\$ 2.61$ from the previous day's close. Let $x$ represent the closing price on May 4. Write an equation for the current day's closing price as the previous day's closing price plus the change.
Substitute values from the chart.

$$
\begin{aligned}
x+2.61 & =52.20 \\
-2.61 & =-2.61 \\
\hline x & =49.59
\end{aligned}
$$

$$
\text { Subtract } 2.61 \text { from each side of the equation. } \quad \underline{-2.61=-2.61}
$$

XYZ Corporation closed at $\$ 49.59$ on May 4.

## CHECK YOUR UNDERSTANDING

At what price did XYZ Corporation close on May 11?

## EXAMPLE 4

- Use the May 4 closing price from Example 3 and the May 5 opening price to find the difference in prices as a percent increase. Round to the nearest hundredth percent.
SOLUTION The percent increase of one share of stock for these two prices can be calculated by using the following formula.

$$
\text { Percent increase }=\frac{\text { Open }- \text { Close }}{\text { Close }} \times 100
$$

Substitute values from the chart. $\quad \frac{50.10-49.59}{49.59} \times 100$
Simplify the fraction. $0.010284 \times 100$
Multiply. Then round.
1.03

There was approximately a $1.03 \%$ increase in the price per share of XYZ Corporation due to after-hours trading.

CHECK YOUR UNDERSTANDING
Use the May 11 closing price from the previous Check Your Understanding and the May 12 opening price to represent the difference as a percent decrease. Round to the nearest hundred percent.

## EXAMPLE 5

On May 6, the XYZ Corporation announced a decrease in earnings. This news caused the price of their stock to drop. It closed at $\$ 44.37$. Express the net change from May 5 to May 6 as a percent.

SOLUTION You can find the net change using the following formula.
Net change
$\frac{\text { May } 6 \text { close }- \text { May } 5 \text { close }}{\text { May } 5 \text { close }} \times 100$
Substitute values from the chart.
$\frac{44.37-52.20}{52.20} \times 100$
Simplify the fraction.
$-0.15 \times 100$
Multiply.
-15\%
The net change expressed as a percent is $-15 \%$. This means the closing price on May 6 reflects a $15 \%$ decrease from the closing price on May 5.

## CHECK YOUR UNDERSTANDING

On May 13, the XYZ Corporation announced another decrease in earnings. The price of their stock dropped to close at $\$ 45.72$. Express the net change from May 12 to May 13 as a percent, to the nearest tenth.

## Spreadsheets

A spreadlsheet is an electronic worksheet that can be used to keep track of stock information. Spreadsheets allow you to enter data into columns and rows. The intersection of a column and a row is a celll. Cells can contain numbers, words, or formulas. While the structure of a formula may differ based on the software, formulas have a fundamental algebraic basis. In spreadsheet formulas you use an * (asterisk) for the multiplication symbol and a / (forward slash) for the division symbol. Do not use spaces around symbols.

Examine the spreadsheet below that contains information on the XYZ Corporation for May 4-May 6. Columns are named using letters of the alphabet, while rows are numbered. Because a cell is the intersection of a column and a row, a cell is named with its column letter and row number.

| cell D4 |  | A | B | C | $D$ | $E$ | $F$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | XYZ CORP |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |
| 3 | Date | High | Low | Close | Change | \% Change |  |
| 4 | 4-May | 50.23 | 49.34 | 49.59 |  |  |  |
| 5 | 5-May | 52.60 | 49.00 | 52.20 |  |  |  |
| 6 | 6-May | 52.20 | 40.78 | 44.37 |  |  |  |

The closing price for May 4 is in cell D4. A formula can be stored in cell E5 to calculate the net change. Think of each cell name as a variable. If E5 represents the net change of the closing price from May 4 to May 5, the equation needed is E5 = D5 - D4. You enter the right side of the equation in cell E5 beginning with the = symbol. The formula uses the values in cells D5 and D4 to calculate the net change for May 5 and stores it in cell E5.

|  | A | B | C | D | $E$ | $F$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | XYZ CORP |  |  |  |  |  |
| 2 |  |  |  |  |  |  |
| 3 | Date | High | Low | Close | Change | \% Change |
| 4 | 4-May | 50.23 | 49.34 | 49.59 |  |  |
| 5 | 5-May | 52.60 | 49.00 | 52.20 | 2.61 |  |
| 6 | 6-May | 52.20 | 40.78 | 44.37 |  |  |

## EXAMPLE 6

: Write a formula for cell F6 to calculate the percent net change for May 6.
: SOLUTION The percent net change from May 5 to May 6 was calculated in Example 5. The formula uses the May 5 and May 6 closing prices. These prices are in cells D5 and D6, respectively. Use the cell names as the variables and multiply by 100 to get a percent.
Substitute cell names into formula. $\frac{\mathrm{D} 6-\mathrm{D} 5}{\mathrm{D} 5} \times 100$
Convert to a spreadsheet formula. =(D6-D5)/D5*100

|  | A | B | C | $D$ | $E$ | $F$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | XYZ CORP |  |  |  |  |  |
| 2 |  |  |  |  |  |  |
| 3 | Date | High | Low | Close | Change | \% Change |
| 4 | 4-May | 50.23 | 49.34 | 49.59 |  |  |
| 5 | 5-May | 52.60 | 49.00 | 52.20 | 2.61 |  |
| 6 | 6-May | 52.20 | 40.78 | 44.37 |  | $-15^{2}$ |

Order of Operations Notice there is only one set of parentheses in the formula. Following the order of operations, division by D5 occurs before multiplication by 100 . However, it is necessary to enclose the numerator in parentheses so the difference D6 - D5 is divided by D5. Without those parentheses, the spreadsheet first divides D5 by D5, then multiplies that quotient by 100, and finally subtracts that answer from D6, which results in an incorrect value.

Rounding You can set the number of rounding places for each cell according to the degree of accuracy needed in your calculations. Be aware that the computer retains the entire calculation to many decimal places. In this case, it just shows the value to two decimal places.

## CHECK YOUR UNDERSTANDING

Write formulas for cells E6 and F5 in the spreadsheet above.

## Applications

## One of the funny things about the stock market is that every

time one person buys, another sells, and both think they are
astute.

## William Feather, Publisher and Author

1. Why might the buyer and seller of the same stock both think that their trading price was an "astute" decision? How might those words apply to what you have learned?

Use the following information posted at the end of the trading day on April 22 to answer Exercises 2-7.

| 52-week <br> High | 52-week <br> Low | Symbol | Stock | Last | Change | Sales of <br> 100s | High | Low |
| :---: | :---: | :---: | :--- | ---: | ---: | ---: | ---: | :---: |
| 151,650 | 107,200 | BRK/A | Berkshire <br> Hathaway Inc | 127,200 | -1000 | 4.11 | 128,600 | 127,000 |
| 120.2 | 66.39 | FCX | Freeport-McMoRan <br> Copper \& Gold Inc | 118.65 | 3.51 | 147,540 | 120.06 | 116.64 |
| 63.69 | 46.64 | MCD | McDonald's <br> Corporation | 58.35 | -0.55 | 106,077 | 58.77 | 57.42 |
| 266.81 | 112.11 | PTR | PetroChina <br> Company Ltd | 137.19 | +2.16 | 16,266 | 140.92 | 136.09 |
| 39.63 | 27.51 | TXN | Texas Instruments Inc <br> Westpac Banking | 28.85 | -11.74 | 288,012 | 29.64 | 28.38 |
| 144.04 | 92.18 | WBK | Worporation | 2.45 | 332.7 | 115.35 | 113.50 |  |

2. What was the difference between the 52 -week high and 52 -week low price for one share of PetroChina Company Ltd?
3. What is the difference between the day's high and low prices for McDonald's Corporation?
4. Determine the volume for each of the following stocks.
a. Berkshire Hathaway Inc
b. McDonald's Corporation
c. Texas Instruments Inc
d. Westpac Banking Corporation
5. Determine the closing price on April 21 for each of the following stocks.
a. Texas Instruments Inc
b. Freeport-McMoRan Copper \& Gold Inc
6. Use the information from Exercise 5 to determine the percent of net change from April 21 to April 22 for each of the corporations listed in that question. Round answers to the nearest tenth of a percent.
7. On April 22, which stock(s) had a daily high that was approximately $50 \%$ lower than the 52 -week high?
8. If the April net change for Westpac Banking Corporation was -3.03 , what was the closing price for that day?
9. Which of the following is a true statement? Explain your reasoning.

The 52-week high can never be higher than the day's high.
The day's high can never be higher than the 52-week high.
10. At the end of the trading day on April 25 , Texas Instruments Inc closed at $\$ 28.84$, which was a $+5.22 \%$ net change from the previous day's close. What was the approximate close on the previous day?
11. On April 25, Berkshire Hathaway Inc closed at $\$ 126,875$ per share. One year earlier, one share closed at $\$ 108,750$. What was an approximate one-year percent change?

Use the spreadsheet below to answer Exercises 12-16.

|  | A | B | C | D | E | F | G | H |
| :--- | :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | Symbol | Stock | April 25 <br> Last | Change | $\%$ Change | April 24 <br> Close | Volume in <br> 1,000s | Volume in <br> 100s |
| 2 | AAPL | Apple Inc | 169.73 | 0.79 |  | 168.94 | 35,445 |  |
| 3 | BBW | Build-A-Bear <br> Workshop Inc | 10.15 | 1.15 | $12.78 \%$ |  | 616 |  |
| 4 | CTB |  <br> Rubber Co | 14.7 | -1.82 |  | 16.52 | 2,671 |  |
| 5 | F | Ford Motor Co | 7.5 | -0.9 |  |  | 227,269 |  |
| 6 | INTC | Intel Corp | 22.56 |  | $-0.57 \%$ |  | 47,604 |  |
| 7 | MSFT | Microsoft Corp | 29.83 |  | $-6.19 \%$ | 31.80 | 145,194 |  |
| 8 | NTGR | NETGEAR Inc | 16.76 | -3.37 | $-16.74 \%$ |  | 8,085 |  |
| 9 | YHOO | Yahoo! Inc | 26.8 |  | $-1.83 \%$ |  | 50,523 |  |

12. Write a formula that will convert the volume given in 1,000 s into a volume given in 100s. Use the left side of the equation to indicate in which cell to store the formula.
a. Intel Corp
b. Yahoo! Inc
13. Write a formula that will store the exact volume for each stock in column I. Use the left side of the equation to indicate in which cell to store the formula.
a. Build-A-Bear Workshop Inc
b. NETGEAR Inc
14. Write a formula to determine the close on April 24 for each of the following. Use the left side of the equation to indicate in which cell to store the formula.
a. NETGEAR Inc
b. Ford Motor Co
15. Write a formula to determine the percent change for each of the following. Use the left side of the equation to indicate in which cell to store the formula.
a. Apple Inc
b. Cooper Tire \& Rubber Co
16. Write a formula to determine the net change for each. Use the left side of the equation to indicate in which cell to store the formula.
a. Microsoft Corp
b. Cooper Tire \& Rubber Co

## 1-3

## Objectives

- Interpret a stock bar chart.
- Create a stock bar chart.
- Interpret a stock candlestick chart.
- Create a stock candlestick chart.


## Key Terms

- stock chart
- stock bar chart
- candlestick chart


## How can stock data be displayed?

Data can be presented in list form or in graphical form. The graphical form is known as a stock chart. These charts offer pictorial information on anything from a day's worth of data to multiyear data trends. Most stock charts present historical information about the trading prices and volumes of a particular stock.

A common stock chart format is the stock lbar chart. The chart below shows price and volume information for General Electric on April 30.

Notice the chart consists of two graphs. The top portion shows daily information about the day's high, low, open, and close prices. The bottom portion shows the daily volume for that stock.

The top shaded bar is a rectangle formed between the day's low and high. The line segment on the left side of the rectangle is positioned at the day's opening price and the line segment on the right side is positioned at the day's closing price.

The bottom shaded bar starts at 0 and rises to the approximate number of shares traded on that date. Notice that the scale for this particular portion of the chart is in millions, although it could be in hundreds or thousands depending upon the range in the volume. Stock bar charts can also be used to show the market action on multiple days.

## Skills and Strategies

Here you will learn how to interpret and create stock charts. The stock bar chart below presents trading information for the week of April 28 for Ford Motor Company.

## EXAMPLE 1

: Which day had the greatest high price? Which day had the least low price?
SOLUTION The top portion of the chart shows the day's trading prices. Because the top of each bar represents the day's high price, the greatest high for the week was on May 2.

The bottom of each bar represents the day's low price, so the lowest low for the week occurred on April 29.

## CHECK YOUR UNDERSTANDING

Between which two days did afterhours trading appear to have the biggest impact on the difference between the closing price and the following day's opening price?

## EXAMPLE 2



- Approximately how many shares of Ford

Motor Company were traded over the five-day period?
SOLUTION The bottom portion of the chart shows the daily volume of shares traded. The scale is in millions of shares. While it is not possible to give an exact accounting of each day's volume, you can determine approximations of these amounts.
For April 28, the top of the volume bar reaches at a point slightly higher than half the distance between the 150 million and 200 million lines. An approximation of the day's volume is 185 million shares.
For April 29, the volume appears to be slightly above the 50 million line. So an approximation is 60 million shares.
Approximations for the rest of the week's trading volumes are 65 million, 60 million, and 90 million.

Add the five approximations. $\quad 185+60+65+60+90=460$
About 460,000,000 shares of Ford Motor Company were traded during

- the week of April 28.


## CHECK YOUR UNDERSTANDING

Use the stock bar chart to write a brief financial story of the trading action that occurred for Ford Motor Company on April 28 and April 29. Begin your story with "On April 28, one share of Ford Motor Company opened at $\$ 8.15$. During the day . . ."

## EXAMPLE 3

: Use the information below to construct a one-day stock bar chart. Open: $\$ 40.10 \quad$ Close: $\$ 39.79$

High: $\$ 40.65$ Low: $\$ 39.39 \quad$ Volume: 44,500,000
SOLUTION Determine an appropriate interval to use to display the information. The range of the daily prices is from $\$ 39.39$ to $\$ 40.65$. Therefore, choose a value to begin the interval that is less than the lowest price and a value to end the interval that is greater than the highest price. Use $\$ 39.25$ to $\$ 40.75$. Next, establish interval amounts that are easy to read. Use intervals of $\$ 0.25$.

Draw a rectangle whose bottom is positioned at the low for the day and top at the high for the day. Draw a line to the left of the rectangle that is approximately at the opening price and a line to the right of the rectangle that is approximately at the closing price.


Next construct the volume portion of the chart. Select a suitable interval in millions, in this case 0 to 50 . Beginning at 0 , construct a bar that rises to the approximate volume for the day.

These two portions form a one-day stock bar chart.

## CHECK YOUR UNDERSTANDING

Suppose that trading was suspended for one entire day for a corporation. What might the stock bar chart look like?

## Candlestick Charts

Another type of chart that is similar to a stock bar chart is a candllesticlk chart. A candlestick chart may be easier to read and contains more information at a glance. The top and bottom of the vertical line indicate the high and low prices over the given time period. The rectangular region is known as the real body and is displayed in two different colors depending upon the action for the day on that stock.
 can be customized. The candlestick chart for Sept. 7-11 depicts market action for a particular stock for five days in September. The green candlestick indicates that the closing price is greater than the opening price. The red candlestick indicates the opposite; the closing price is less than the opening price.

Candlestick Chart, Sept. 7-11

## EXAMPLE 4

: Explain the difference between the market action on

- September 8 compared to September 9 shown in the candlestick chart for Sept. 7-11.
SOLUTION The candlestick is green on September 8, which means the closing price for the day was higher than the opening price. The red candlestick on September 9 indicates that the opening price for the day was higher than the closing price.


## CHECK YOUR UNDERSTANDING

Interpret a green candlestick that is shown as only a rectangle with no lines at the top or bottom.


## EXAMPLE 5

What was the approximate difference between the highest price and the lowest price for the week shown in the candlestick chart for Sept. 7-11?
SOLUTION The highest price for the week, approximately $\$ 39.90$, occurred on September 7 as indicated by the highest portion of any of the candlesticks.
The lowest price for the week, approximately $\$ 37.75$, occurred on September 11 as indicated by the lowest portion of any of the candlesticks.
The difference between the week's high and low prices is
approximately $\$ 39.90-\$ 37.75$, or $\$ 2.15$.

## CHECK YOUR UNDERSTANDING

The lengths of the candlesticks for September 8 and 11 are approximately the same. What does this mean about the trading prices on both of those days?

## Applications

## Although it's easy to forget sometimes, a share is not a lottery

ticket . . . it's part-ownership of a business.
Peter Lynch, American businessman, Investment strategist, and Philanthropist

1. How might those words apply to what you have learned? Why is the author warning readers that a share is not a lottery ticket?
The following stock bar chart depicts the market action for The Washington Post Company during the week of April 28. Use the chart to answer Exercises 2-11.

2. On what date did the stock close at a price higher than it opened?
3. What was the day's opening price on the following days?

April 28
April 29
April 30
May 1
May 2
4. What was the day's high price on April 29?
5. What was the day's low price on May 1?
6. What was the day's close on May 2 ?
7. What was the approximate net change from April 29 to April 30? Express that net change as a monetary amount and as a percent to the nearest tenth.
8. What was the approximate net change from April 30 to May 1? Express that net change as a monetary amount and as a percent to the nearest tenth.
9. Approximately how many shares were traded on April 30?
10. Approximately how many fewer shares were traded on April 28 than on May 2?
11. Suppose that the volume numbers had been listed in hundreds on the table. How would that have changed the labels?
12. Use the following data to construct a stock bar chart for the 5-day period.

| Day | Open | Close | High | Low | Volume |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 20.48 | 20.24 | 20.50 | 20.20 | $58,000,000$ |
| 2 | 20.21 | 20.25 | 20.30 | 20.00 | $52,000,000$ |
| 3 | 20.30 | 20.10 | 20.34 | 20.02 | $42,000,000$ |
| 4 | 20.17 | 20.44 | 20.45 | 20.10 | $50,000,000$ |
| 5 | 20.48 | 20.61 | 20.65 | 20.36 | $50,000,000$ |

13. Use the following data to construct a stock bar chart for the 5-day period.

| Day | Open | Close | High | Low | Volume |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 59.75 | 59.60 | 60.00 | 59.22 | $7,900,000$ |
| 2 | 59.15 | 60.20 | 60.50 | 59.15 | $8,000,000$ |
| 3 | 60.00 | 59.58 | 60.61 | 59.55 | $8,200,000$ |
| 4 | 59.55 | 60.90 | 60.90 | 59.37 | $7,000,000$ |
| 5 | 60.87 | 60.93 | 61.25 | 60.79 | $7,750,000$ |

14. Use the candlestick chart to answer the questions.
a. On which days were opening prices higher than the closing prices?
b. On which days were the closing prices higher than the opening prices?
c. What was the approximate closing price on April 28?
d. What was the approximate high price on May 1?
e. What was the difference between the lowest price and the highest price recorded for this time period?


|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| April |  |  |  | May |
| 27 | 28 | 29 | 30 | 1 |

f. What does the very short line at the bottom of the May 1 candlestick indicate?
g. Had the chart used white and black candlesticks, which days would be white and which days would be black?
h. On which consecutive days was the closing price of the first day higher than the opening price of the second day?
15. Construct a candlestick chart for the information presented in Exercise 12.
16. Construct a candlestick chart for the information presented in Exercise 13.

## 1-4 <br> Simple Moving Averages

## Objectives

- Understand how data is smoothed.
- Calculate simple moving averages using the arithmetic average formula.
- Calculate simple moving averages using the subtraction and addition method.
- Graph simple moving averages using a spreadsheet.


## Key Terms

- smoothing techniques
- simple moving average (SMA)
- arithmetic average (mean)
- lagging indicators
- fast moving average
- slow moving average
- crossover


## How can stock data be smoothed?

Stock market prices can fluctuate greatly from trade to trade based upon a variety of external factors. You have already seen that the high and low for a day may not necessarily be near the day's opening or closing prices. Those differences often make it difficult to spot trends that are occurring over time. Smoothing techmiques are statistical tools that allow an investor to reduce the impact of price fluctuations and to focus on patterns and trends. One such technique is known as a simple moving average (SMA). Simple moving averages are calculated by determining the arithmetic average (mean) closing price over a given period of time.

The graph shows the daily stock closing prices, 5-day SMA and 10 -day SMA over a period of 30 trading days. Notice how the closing prices fluctuated from day to day and the moving average graphs smoothed out that data. The longer the moving average time interval, the smoother the graph appears to be.

Moving aver-
 ages are known as lagging indicators because they use past data. Investors use simple moving averages when they want to identify and follow a trend in prices.

Recall that the average of a set of numerical data is the sum of the items in that set divided by the number of items. You can determine the average of any number of closing prices, but this gives you little information about trends because you would have nothing to compare the averages to. A better comparison method to use is a simple moving average.

## Simple Moving Averages Using the Arithmetic Average Formula

Although simple moving averages can span any length of time, in Example 1 you will find averages by taking closing prices 5 days at a time. Find an average of the prices for each of the 5 -day time spans: days $1-5$, days $2-6$, days $3-7$, days $4-8$, days $5-9$, and days $6-10$. Graph the six averages. The graph has a smoother appearance compared to the graph of the closing prices of days 5-10. A moving average graph appears to smooth the fluctuations in closing prices.

## EXAMPLE 1

: The closing prices for 10 consecutive trading days for a particular stock are shown. Calculate the 5-day SMA and plot both the closing prices and the averages on a graph.
SOLUTION Find the average of the closing prices in groups of five.
Find the SMA using the closing prices from days 1-5.
$\frac{35.02+35.01+34.65+36.09+35.32}{5}=35.218 \approx 35.22$
Days $2-6 \quad \frac{35.01+34.65+36.09+35.32+35.50}{5}=35.314 \approx 35.31$
Days 3-7 $\frac{34.65+36.09+35.32+35.50+35.03}{5}=35.318 \approx 35.32$

| Day | Closing Price |
| :---: | :---: |
| 1 | 35.02 |
| 2 | 35.01 |
| 3 | 34.65 |
| 4 | 36.09 |
| 5 | 35.32 |
| 6 | 35.50 |
| 7 | 35.03 |
| 8 | 35.79 |
| 9 | 37.07 |
| 10 | 36.05 |

Days $4-8 \quad \frac{36.09+35.32+35.50+35.03+35.79}{5}=35.546 \approx 35.55$
Days 5-9 $\frac{35.32+35.50+35.03+35.79+37.07}{5}$

$$
=35.742 \approx 35.74
$$

Days $6-10 \frac{35.50+35.03+35.79+37.07+36.05}{5}$

$$
=35.888 \approx 35.89
$$

The five consecutive 5 -day SMA are $\$ 35.22, \$ 35.31$, $\$ 35.32, \$ 35.55, \$ 35.74$, and $\$ 35.89$.
The graph of the closing prices and the simple moving averages for days 5 through 10 are shown. Notice how the moving averages smooth out the data.


## CHECK YOUR UNDERSTANDING

Closing prices for 10 consecutive trading days were $\$ 55, \$ 60, \$ 62$, $\$ 48, \$ 40, \$ 42, \$ 45, \$ 46, \$ 43$, and $\$ 49$. Calculate the 5 -day SMA. Plot both the closing prices and the averages on a graph.

## Simple Moving Averages Using the Subtraction and Addition Method

The calculation of a simple moving average can be tedious because you have to find the average for each time interval. There is an alternate way to compute the moving average that is simpler.

Suppose you want to determine a 3-day simple moving average for 6 trading days. Let the trading prices for the days be represented by $A, B, C$, $D, E$, and $F$. The trading prices for the first three days are $A, B$, and $C$. The average of those prices is

$$
\frac{A+B+C}{3}=\frac{A}{3}+\frac{B}{3}+\frac{C}{3}
$$

Using the method in Example 1, find the average of days 2-4 using B, $C$, and $D$. This is the same as subtracting price $A$ and adding price $D$, or

$$
\frac{A}{3}+\frac{B}{3}+\frac{C}{3}-\frac{A}{3}+\frac{D}{3}
$$

Rearranging the terms and simplifying, this process is the same as finding the average for days $2-4$.

$$
\frac{A}{3}-\frac{A}{3}+\frac{B}{3}+\frac{C}{3}+\frac{D}{3}=\frac{B}{3}+\frac{C}{3}+\frac{D}{3}=\frac{B+C+D}{3}
$$

## EXAMPLE 2

Use the subtraction and addition method to determine the 4-day SMA for the following closing prices.
\$121, \$122, \$120, \$119, \$124, \$128, \$126
SOLUTION Calculate the average closing prices of days 1-4.
Add the first 4 prices. Divide by 4. $\frac{121+122+120+119}{4}=120.50$
Use subtraction and addition to determine the averages for days 2-5.
Use previous average, $\frac{A}{4}$, and $\frac{E}{4} . \quad 120.50-\frac{121}{4}+\frac{124}{4}=121.25$
Find the averages for days 3-6 and days 4-7.
Use previous average, $\frac{B}{4}$, and $\frac{F}{4} . \quad 121.25-\frac{122}{4}+\frac{128}{4}=122.75$
Use previous average, $\frac{C}{4}$, and $\frac{G}{4} . \quad 122.75-\frac{120}{4}+\frac{126}{4}=124.25$
The simple moving averages are $\$ 120.50, \$ 121.25, \$ 122.75$, and $\$ 124.25$.

## CHECK YOUR UNDERSTANDING

Use the subtraction and addition method to determine the 3-day SMA for the closing prices $\$ 28, \$ 31, \$ 37, \$ 38$, and $\$ 35$.

## EXTEND YOUR UNDERSTANDING

In Example 2, what would the eighth trading day's closing price have to be so that the next moving average remains the same at $\$ 124.25$ ?

## Graph Simple Moving Averages Using a Spreadsheet

Simple moving averages are more informative when they are determined over a longer period of time. Often, financial websites and newspapers report long moving average time intervals. These calculations are time consuming if done by hand or even using a calculator. However, if you use a spreadsheet you can get results easily and quickly. The spreadsheet shown lists the closing prices of 30 consecutive days of trading for a particular stock. The 10-day moving averages are calculated in column C and begin on day 10. Cell C11 equals the average of the closing prices on days $1-10$.

Most spreadsheets have a sum function, which is used to calculate the sum of amounts in a group of cells. The format for using a sum function varies depending on the spreadsheet software you are using. The format used here is =sum(starting cell:ending cell). The formula in cell C11 that yields the correct average is $=\operatorname{sum}(\mathrm{B} 2: \mathrm{B} 11) / 10$. The cells have been formatted to show all decimals rounded to two places.

The formula in cell C12 is $=\operatorname{sum}(B 3: B 12) / 10$. Notice that the starting and ending cells in the formula have each shifted down by one cell. Rather than typing this formula repeatedly and changing the cell names used, most spreadsheets have a fill command that recognizes the pattern. To use this command in this spreadsheet select the cells that you want to fill with the formula and apply the fill command. Most spreadsheets allow the user to fill up, fill down, fill left, or fill right. In this case, you fill down. The formula is placed in each selected cell with the cell names automatically adjusted for each row.

|  | A | B | C |
| ---: | ---: | ---: | ---: |
| 1 | Day | Closing <br> Price | 10-day Moving <br> Average |
| 2 | 1 | 35.02 |  |
| 3 | 2 | 35.01 |  |
| 4 | 3 | 34.65 |  |
| 5 | 4 | 36.09 |  |
| 6 | 5 | 35.32 |  |
| 7 | 6 | 35.5 |  |
| 8 | 7 | 35.03 |  |
| 9 | 8 | 35.79 |  |
| 10 | 9 | 37.07 |  |
| 11 | 10 | 36.05 | 35.55 |
| 12 | 11 | 36.85 | 35.74 |
| 13 | 12 | 38.03 | 36.04 |
| 14 | 13 | 38 | 36.37 |
| 15 | 14 | 37.76 | 36.54 |
| 16 | 15 | 37.66 | 36.77 |
| 17 | 16 | 37.66 | 36.99 |
| 18 | 17 | 38.3 | 37.32 |
| 19 | 18 | 39.48 | 37.69 |
| 20 | 19 | 38.72 | 37.85 |
| 21 | 20 | 39.01 | 38.15 |
| 22 | 21 | 38.48 | 38.31 |
| 23 | 22 | 39.01 | 38.41 |
| 24 | 23 | 38.8 | 38.49 |
| 25 | 24 | 38.19 | 38.53 |
| 26 | 25 | 38.2 | 38.59 |
| 27 | 26 | 37.3 |  |
| 28 | 27 | 37.2 |  |
| 29 | 28 | 37.33 |  |

## EXAMPLE 3

- Use a spreadsheet to calculate the 5-day SMA of the closing prices for 10 consecutive trading days.
SOLUTION Moving averages lag behind the closing prices, so in cell
: C6 calculate the average of the closing prices for April 28, 29, 30, May 1 and 2. The formula is $=\operatorname{sum}(\mathrm{B} 2: \mathrm{B} 6) / 5$.
Next, highlight cells C6 through C11 and apply the fill down command to have the 5-day moving averages appear in the appropriate cells as shown in blue.


## CHECK YOUR UNDERSTANDING

Add column D to the spreadsheet to calculate the 3-day SMA. In what cell do you start? What formula do you use?

|  | A | B | C |
| :---: | :---: | :---: | :---: |
| 1 | Day | Close | Moving <br> Average |
| 2 | 28-Apr | 29.39 |  |
| 3 | 29-Apr | 29.27 |  |
| 4 | 30-Apr | 29.21 |  |
| 5 | 1-May | 29.70 |  |
| 6 | 2-May | 29.08 | 29.33 |
| 7 | 5-May | 29.24 | 29.30 |
| 8 | 6-May | 29.40 | 29.33 |
| 9 | 7-May | 28.52 | 29.19 |
| 10 | 8-May | 28.64 | 28.98 |
| 11 | 9-May | 28.99 | 28.96 |

## Crossovers

Sometimes, investors construct stock charts that depict moving averages for two different intervals. The graph with the shorter time interval is known as the fast moving average and the graph with the longer time interval is known as the slow moving average. As changes in closing prices occur on a day-to-day basis, the fast moving average will reflect those changes quicker than the slow moving average will.

A crossover occurs when a one-time interval moving average graph overtakes another. Crossovers signal that a stock trend reversal might be near. Some say that an investor should consider buying when the fast moving average graph overtakes (rises above) the slow moving average graph. Likewise, an investor might consider selling
 when the fast moving average graph crosses below the slow moving average graph.

## EXAMPLE 4

The graph shows the closing prices for 30 consecutive trading days. It also charts the 7-day and 21-day simple moving averages. What signal might the graphs give an investor?

SOLUTION A crossover occurs on the 27th day. The fast moving average graph rises above the slow moving average graph giving a signal to consider buying the stock.

## CHECK YOUR UNDERSTANDING

Suppose that on the 35th trading day, the 21-day SMA graph rises above the 7 -day graph. What might that indicate?

## Applications

Never try to walk across a river just because it has an average depth of four feet.

Milton Friedman, American economist

1. Why might the author be warning readers to be cautious of averages? How might these words apply to what you have learned?
In Exercises 2-5, use the method illustrated in Example 1 to determine the simple moving averages by repeatedly finding sums.
2. Determine the 3-day SMA for the ten consecutive day closing prices of Sprint Nextel Corp listed below. $\$ 7.78, \$ 8.08, \$ 7.99, \$ 8.02, \$ 7.89, \$ 8.72, \$ 9.19, \$ 9.16, \$ 8.98, \$ 9.38$
3. Determine the 5 -day SMA for the ten consecutive day closing prices for MasterCard Inc listed below.
\$242.50, \$273.98, \$278.16, \$293.94, \$285.04
\$290.80, \$296.02, \$291.01, \$293.41, \$286.85
4. Determine the 4-day SMA for the ten consecutive day closing prices for Wal-Mart Stores Inc listed below.
\$57.35, \$58.61, \$57.98, \$58.07, \$57.50
\$56.97, \$56.35, \$56.83, \$57.16, \$57.18
5. Determine the 6 -day SMA for the twelve consecutive day closing prices for Exxon Mobil Corp listed below.
\$92.60, \$92.46, \$92.45, \$91.79, \$93.07, \$89.70
\$89.61, \$89.51, \$90.07, \$88.82, \$89.93, \$88.82
In Exercises 6-9, use the method illustrated in Example 2 to determine moving averages by subtraction and addition.
6. Determine the 2-day SMA for the ten consecutive day closing prices for Toyota Motor Corp listed below. \$101.96, \$101.80, \$101.50, \$103.07, \$104.94 \$105.12, \$105.66, \$104.76, \$100.56, \$101.31
7. Determine the 3-day SMA for the ten consecutive day closing prices for Procter \& Gamble Co listed below.
\$66.21, \$65.90, \$67.05, \$67.03, \$66.80
\$66.65, \$66.65, \$65.80, \$65.92, \$65.21
8. Determine the 4 -day SMA for the ten consecutive trading day closing prices for International Business Machines Corp listed below.
\$121.69, \$122.85, \$120.70, \$123.61, \$123.18
\$122.03, \$122.82, \$124.14, \$124.92, \$124.06
9. Determine the 6 -day SMA for the ten consecutive trading day closing prices for Rite Aid Corp listed below.
\$2.65, \$2.63, \$2.70, \$2.63, \$2.50, \$2.65, \$2.66, \$2.56, \$2.52, \$2.37
10. Use a spreadsheet to determine the 7-day SMA for Citigroup Inc.

| 7-Apr | 24.60 | 14-Apr | 22.51 | 21-Apr | 25.03 | 28-Apr | 26.81 | 5-May | 25.7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 8-Apr | 23.76 | 15-Apr | 22.80 | 22-Apr | 25.12 | 29-Apr | 26.32 | 6-May | 25.87 |
| 9-Apr | 23.58 | 16-Apr | 23.44 | 23-Apr | 24.63 | 30-Apr | 25.27 | 7-May | 24.48 |
| 10-Apr | 23.71 | 17-Apr | 24.03 | 24-Apr | 25.76 | 1-May | 25.99 | 8-May | 24.30 |
| 11-Apr | 23.36 | 18-Apr | 25.11 | 25-Apr | 26.60 | 2-May | 26.39 | 9-May | 23.63 |

11. Use a spreadsheet to determine the 10 -day SMA for Dell Inc.

| 31-Mar | 19.92 | 8-Apr | 19.00 | 16-Apr | 18.72 | 24-Apr | 19.14 | 2-May | 19.32 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1-Apr | 20.33 | 9-Apr | 18.69 | 17-Apr | 19.05 | 25-Apr | 19.11 | 5-May | 19.10 |
| 2-Apr | 19.95 | 10-Apr | 18.77 | 18-Apr | 19.47 | 28-Apr | 18.87 | 6-May | 19.19 |
| 3-Apr | 20.12 | 11-Apr | 18.50 | 21-Apr | 19.56 | 29-Apr | 18.97 | 7-May | 18.90 |
| 4-Apr | 19.53 | 14-Apr | 18.24 | 22-Apr | 19.05 | 30-Apr | 18.63 | 8-May | 18.84 |
| 7-Apr | 19.23 | 15-Apr | 18.28 | 23-Apr | 19.05 | 1-May | 19.08 | 9-May | 19.03 |

12. Use a spreadsheet to determine the 2-day, 3-day, and 5-day SMA.

| 31-Mar | 4 | 8 | 46 | 16-Apr | 455.03 | 2 | 543.04 | 2-May | 581.29 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1-Apr | 465.71 | 9-Apr | 464.19 | 17-Apr | 449.54 | 25-Apr | 544.06 | 5-May | 594.90 |
| -Ap | 465.70 | 10-Ap | 469.08 | 18-Apr | 539.41 | 28-Apr | 55. | 6-May | 586.36 |
| $3-A p r$ | 455.12 | 11-Apr | 457.45 | 21-Apr | 537.79 | 29-Apr | 558.47 | 7-May | 579.00 |
| 4-Apr | 471.09 | 14-Apr | 451.66 | 22-Apr | 555.00 | 30-Apr | 574.29 | 8-May | 583.01 |
| 7-Apr | 476.82 | 15-Apr | 446.84 | 23-Apr | 546.49 | 1-May | 593.08 | 9-May | 573.20 |

13. The stock chart shows the 3 -day and 10-day SMA for 20 consecutive trading days of Sony Corp stock. Identify the crossovers and discuss the implications.


14. The stock chart shows the 3 -day, 5 -day, and 10 -day SMA for 16 consecutive trading days of General Electric Co stock. Examine days 6-16. Identify the crossovers and discuss the implications.
15. Use a spreadsheet to calculate the 2-day and 5-day SMA for ten consecutive day closing prices of Yahoo! Inc. Graph the closing prices and averages.

| 21-Apr | 28.55 | 1-May | 26.81 |
| :--- | :--- | :--- | :--- |
| 22-Apr | 28.54 | 2-May | 28.67 |
| 23-Apr | 28.08 | 5-May | 24.37 |
| 24-Apr | 27.30 | 6-May | 25.72 |
| 25-Apr | 26.80 | 7-May | 25.64 |
| 28-Apr | 26.43 | 8-May | 26.22 |
| 29-Apr | 27.36 | 9-May | 25.93 |
| 30-Apr | 27.41 |  |  |

## Stock Market Ticker <br> 1-5

## Key Terms

- Dow Jones Industrial Average (DJIA)
- ticker
- stock symbol
- ticker symbol
- trading volume
- trading price
- directional arrow
- total value of a trade
- uptick
- downtick
- money flow
- positive money flow
- negative money flow
- daily money flow
- net money flow


## How is stock market data

 TRANSMITTED TO THE INVESTOR?
## Objectives

- Understand stock market ticker information.
- Determine the total value of a trade from ticker information.
- Determine trade volumes from ticker information.

Investors are always interested in how the market is doing. You can refer to a variety of published information systems to track the performance of certain types of stocks. Perhaps the most well-known of these systems is the Dow Jones Indlustrial Average (IDJIA), also known as the Dow. The Dow follows the daily trading action of 30 large public companies. Historically, these were industrial companies, but the corporations included in the Dow have grown to include those in telecommunications, pharmaceuticals, broadcasting, retail, insurance, and more. The Dow is a well-respected average that offers a broad picture of how the market is performing from day to day.

Investors wanting specific information often turn to another source. One of the first stock information transmission machines was invented by Thomas Edison in 1869. It was known as the Universal Stock Ticker and had a printing speed of about one character per second. The machine was known as a ticker because of the ticking sound that it made as printed tape came out of it. This ticker tape machine replaced the need for handwritten and hand-delivered messages about stock trades. Stock tickers in different buildings were connected by telegraph machines. The printed tape would contain a ticker symbol that was unique to a given company. Once the company was identified by the symbol, the ticker would print information about the number of shares traded, the price of that trade, and any change in the direction of the price of a share of the stock. While actual stock ticker machines are now a thing of the past, the idea of transmitting this important information is not. Ticker machines have been replaced by electronic scrolling information that appears on electronic billboards, computers, and TV screens. Many financial TV programs have stock information scrolling across the bottom of the screen during the trading day.

Stock tickers let you know that a stock transaction (trade) has occurred. The ticker offers the following information in coded format.

- Stock Symboll or Ticker Symbol The letter or letters used to identify a corporation whose shares are traded on a stock market are stock symbols or ticker symbols. Stocks that trade on the New York Stock Exchange have 1-, 2-, or 3-letter symbols. Stocks that trade on the NASDAQ had only 4-letter symbols until recently when stocks that transferred to the NASDAQ from the NYSE were allowed to keep their symbols even if fewer than 4 letters.
- Trading Volume The trading volume is the number of shares traded in a single transaction. Trading volumes are listed on the ticker using a shorthand information system. For example, 10K indicates that 10,000 shares traded, 10 M indicates that $10,000,000$ shares traded, and 10B means that $10,000,000,000$ shares traded (rarely seen).
- Trading Price The trading price per share may be displayed on the ticker preceded by the @ symbol, meaning that each share was traded at the specified price. The @ symbol is not always used.
- Directionall Arrows Arrows indicate whether the traded price of a single share is greater than the previous day's closing price ( $\mathbf{(})$ or less than the previous day's closing price ( $\mathbf{\nabla}$ ).


The following examples show how to interpret stock ticker information.

## EXAMPLE 1

Marcy is following the stock market ticker scrolling across the bottom of her TV screen on cable business station. She had purchased some shares of Visa, Inc. last week and is interested in seeing if there are any current trades. She knows that Visa, Inc. has the ticker symbol V. She saw the following information: V 12K@87.37 © 0.12. What can Marcy learn from this line of symbols?

SOLUTION The letter V indicates that a trade has been made for a certain amount of Visa shares. The next piece of information, 12K, indicates that the volume of the most recent trade was 12 thousand shares. Each of those shares was traded at $\$ 87.37$. This price was up $\$ 0.12$ from the previous day's closing price of one share of Visa, Inc.

## CHECK YOUR UNDERSTANDING

Kevin knows that General Electric has the ticker symbol GE. What can Kevin learn from the following line of symbols: GE $12 \mathrm{~K} @ 73.72 \boldsymbol{\nabla} 0.55$ ?

## EXTEND YOUR UNDERSTANDING

Had the trading price of this transaction been at $\$ 87.35$, what number would have appeared after the directional arrow? Explain your answer.

## EXAMPLE 2

: Tom needed money for graduate school tuition. He called his broker and asked her to sell all 3,000 of his Coca-Cola (KO) shares on Wednesday as soon as the trading price hit $\$ 57$ per share. Tom knew that Coca-Cola closed at $\$ 57.25$ on Tuesday. How will his trade appear on the ticker?
SOLUTION Tom is selling 3,000 shares, so the volume is 3 K . The sale price of $\$ 57$ is down from the previous day's close by $\$ 0.25$. This trade appears as KO 3K@57 $\boldsymbol{\mathrm { V }} 0.25$.

## CHECK YOUR UNDERSTANDING

What would be the previous day's close for a share of Coca-Cola if the ticker had read KO 3K@57 ^ 0.25?

## Total Value of a Trade

The totall value of a trade is determined by multiplying the number of shares traded by the trading price. This value does not include any fees.

## EXAMPLE 3

: Toni purchased 15,000 shares of stock of Target Corporation at
: $\$ 54.88$ per share. Her trade appeared on the stock ticker as

- TGT 15K@54.88 $\boldsymbol{\nabla} 0.17$. What was the total value of her trade?

SOLUTION Each of the shares cost Toni $\$ 54.88$. Multiply the number of shares by the price to find the total value of her trade.

Number of shares $\times$ price $15,000 \times 54.88=823,200$
The total value of her trade was $\$ 823,200$.

## CHECK YOUR UNDERSTANDING

Suppose Toni made her purchase at the previous day's closing price.
What would have been the difference between the values of the trades?

## Trade Volume

Trade volume can appear in decimal formats on the stock ticker. For example, 2.5 K is 2.5 thousand, or $2.5 \times 1,000$, or 2,500 . The volume of $3,890,000$ shares can be expressed in ticker notation by using the symbol M to represent millions. To determine the number of millions in $3,890,000$, divide by $1,000,000$. Moving the decimal left 6 places, $3,890,000$ is 3.89 million and is symbolized as 3.89 M .

## EXAMPLE 4

: Grandpa Rich left his three grandchildren: Nicole, Jeff, and Kristen, : 8,750 shares of Apple Inc (AAPL) in his will. The grandchildren sold all - of the shares at a price of $\$ 190.30$ on Friday. The closing price of Apple on Thursday was $\$ 187.83$. How did this trade appear on the stock ticker?
SOLUTION Divide the total number of shares by 1,000. Moving the - decimal point 3 places to the left, 8,750 equals 8.75 thousand. The
: volume of 8,750 shares is 8.75 K on the ticker. Because the shares were sold on Friday at a price that was $\$ 2.47$ higher than the previous day's close, an upward directional arrow indicates the increase. The trade appeared on the ticker as follows: AAPL 8.75K@190.30 © 2.47.

## CHECK YOUR UNDERSTANDING

Express 0.15 M shares traded using the K symbol.

## Customized Tickers

Some stock traders follow customized tickers that offer trade-to-trade information. The term tick is used whenever there is a change in the price of a share from one trade to the next. A trade is an uptick if the price is higher than the previous trade. A trade is a downtick if the price is lower. These tick changes contribute to a type of market analysis known as money flow. When a stock is purchased at an uptick, it is positive money fllow. When it is purchased at a downtick, it is negative money flow.

Dailly money flow is a calculated indicator that is the average of a day's high, low, and close, multiplied by the volume for the day. This calculation can be compared with that for the previous trading day and indicates whether there was a positive or negative money flow. If more shares were bought on the uptick than the downtick, net money flow is positive because more investors were willing to pay a price above the market price.

## EXAMPLE 5

- Laura is interested in trades of Microsoft (MSFT). She has been following the upticks and downticks for the past two days. She knows that MSFT closed on Tuesday at $\$ 20.68$, with a high at $\$ 21.25$ and a low at $\$ 20.50$. There were $11,902,000$ shares traded on that day. She found that Monday's closing price was $\$ 21.23$. The high was $\$ 21.30$ and the low was $\$ 19.95$. The volume for Monday was $16,537,000$ shares. Was the net money flow from Monday to Tuesday positive or negative? SOLUTION Calculate the average of each day's high, low, and close, and then multiply that by the daily volume.


There is a negative net money flow from Monday to Tuesday.

## CHECK YOUR UNDERSTANDING

Let $H$ represent a day's High, $L$ represent a day's Low, $C$ represent a day's close, and $V$ represent the day's volume. Write a formula that can be used to determine the day's money flow.

## Applications

The average trade of an individual is in the thousands of shares， whereas the institutional trade can be in the millions of shares． Clearly，the bigger the order，the bigger the move in the stock． Maria Bartiromo，Business news anchor

1．How might a large trade＂move the market＂？How might those words apply to what you have learned？

Use the following ticker information to answer Exercises 2－9．The stock symbols represent the following corporations：HD，Home Depot Inc； S，Sprint Nextel Corporation；VZ，Verizon Communications Inc；and XOM，Exxon Mobil Corp．

```
HD 32.3M@29.13^1.13 S 1.1K@9.14『0.78 VZ 3.32K@38.77^2.27 XOM 0.66K@92.67『1.58
```

2．Jessica put in an order for some shares of Exxon Mobil Corp．
a．As shown on the ticker，how many shares did Jessica buy？
b．How much did each share cost？
c．What was the value of Jessica＇s trade？
3．Phil sold his shares of Verizon Communications Inc，as indicated on the above ticker．
a．How many shares did he sell？
b．How much did each share sell for？
c．What was the total value of all the shares Phil sold？
4．How many shares of Home Depot are indicated on the ticker？
5．What is the total value of all of the Sprint Nextel Corporation shares traded？

6．How can＠ 29.13 be interpreted？
7．How can XOM ．66K be interpreted？
8．How can $\nabla 1.58$ be interpreted？
9．What was the previous day＇s closing price for each stock？
Use the following ticker to answer Exercises 10－17．The stock symbols represent the following corporations：PG，Procter \＆Gamble Co；BAC， Bank of America Corp；DIS，Walt Disney Co；and K，Kellogg Co．

PG 4．5K＠66．75『0．39 BAC 0．65M＠36．17』0．54 DIS 2．55K＠34．90『1．08 K 0．76K＠51．49ヘ0．04
10．Michele is following the trades of Procter \＆Gamble Co on the busi－ ness channel．The result of the latest trade is posted on the ticker above．
a．How many shares of PG were traded？
b．How much did each share cost？
c．What was the value of the Procter \＆Gamble Co trade？
d．Suppose that the next PG trade represents a sale of 23,600 shares at a price that is $\$ 0.18$ higher than the last transaction．What will Michele see scrolling across her screen for this transaction？
11. Sarah sold her Disney shares as indicated on the ticker.
a. How many shares did she sell?
b. How much did each share sell for?
c. What was the total value of all the shares Sarah sold?
d. Suppose that the next DIS trade that comes across the ticker represents a sale of 7,600 shares at a price that is $\$ 0.98$ higher than the last transaction. What will Sarah see scrolling across her screen for this transaction of DIS?
12. How many shares of Kellogg Co. are indicated on the ticker?
13. What is the total value of all of the Bank of America shares traded?
14. How can @36.17 be interpreted?
15. How can $K 0.76 \mathrm{~K}$ be interpreted?
16. How can $\triangle 0.04$ be interpreted?
17. What was the previous day's closing price for each stock?
a. Procter \& Gamble Co
b. Bank of America Corp
c. Walt Disney Co
d. Kellogg Co
18. Write the ticker symbols for each situation.
a. 36,000 shares of ABC at a price of 37.15 which is $\$ 0.72$ higher than the previous day's close
b. 1,240 shares of XYZ at a price of $\$ 9.17$, which is $\$ 1.01$ lower than the previous day's close
19. Maria is a stock broker and has been following transactions for Ford Motor Co (F). On Tuesday, the last trade of the day for Ford was posted on the ticker as $\$ 8.11$. On Wednesday, the last trade of the day was $\$ 0.56$ higher than Tuesday's close for a purchase of 5600 shares of Ford. Write the stock ticker symbols that would appear on the scroll for the last trade of the day on Wednesday for Ford.
20. Dorothy purchased $x$ thousand shares of Macy's Inc (M) at $y$ dollars per share. This purchase price reflected a decrease of $z$ dollars from the previous day's close. Express the ticket symbols algebraically.
21. Danielle is examining the change in the money flow for Yahoo! Inc shares on two consecutive dates. The information is given in the table. Do the May 16 numbers reflect a positive or negative money flow? Explain.

| Date | High | Low | Close | Volume |
| :---: | :---: | :---: | :---: | :---: |
| 16-May | 27.95 | 27.40 | 27.66 | $53,299,800$ |
| 15-May | 27.90 | 26.85 | 27.75 | $79,670,500$ |

22. Isaac follows the market action of Google Inc. He has watched the prices for two consecutive days. The information he collected is given in the table. Do the June 7 numbers reflect a positive or negative money flow? Explain.

| Date | High | Low | Close | Volume |
| :---: | :---: | :---: | :---: | :---: |
| 7-June | 584.68 | 578.32 | 580 | $4,974,100$ |
| 6-June | 582.95 | 575.60 | 581 | $4,342,700$ |

## Stock Transactions

## Key Terms

- portfolio
- round lot
- odd lot
- trade
- gross capital gain
- gross capital loss


## Objectives

- Learn the basic vocabulary of buying and selling shares of stock.
- Compute gains and losses from stock trades.

A portfolio is a grouping of all the stocks a person currently owns. A portfolio changes whenever stocks are bought or sold. Stocks are best for long-term goals as over time good stocks tend to grow and become more valuable. There are many reasons that stockholders buy or sell shares.

Stocks can go up or down in value. Because some stocks do not perform as planned, it is best to have a diversified portfolio of stocks of different-sized companies in different industries.

When stock is bought and sold, a trade is made with another stockholder. If an investor is buying 600 shares of Xerox Corp, the investor is buying the shares from another shareholder who wants to sell them, not from Xerox Corp. Only the first purchaser of the stock actually bought it from Xerox Corp.

Most shareholders buy and sell stocks in multiples of 100 shares, which are called round lots. A purchase of less than 100 shares is called an oddl lot. When you buy stock, even if its value increases, you will not make a profit until you actually sell the stock. If the shares are sold at a higher price than they were purchased for, you make a profit.

The difference between the selling price and the purchase price is a gross capitall gaim. If you sell a stock for less money than you paid for it, you have a gross capitall loss. You must report capital gains and losses to the Internal Revenue Service because each affects the amount of income taxes owed.

## Skills and Strategies

Investors should keep careful track of the stock market and the stocks in their portfolio, so they know when to buy new stocks, add to what they already own, sell, or just hold on to what they own. Here you will learn how investors determine their capital gains and losses.

## EXAMPLE 1

: Several years ago, Marlene purchased stock for $\$ 7,241$. Last week she sold the stock for $\$ 9,219$. What was her gross capital gain?
SOLUTION Subtract the purchase price from the selling price to find her capital gain.
Selling price - Purchase price $\quad 9,219-7,241=1,978$
Marlene has a gross capital gain of $\$ 1,978$. She must report this as income on her income tax return for the year in which she sold the stock.

## CHECK YOUR UNDERSTANDING

Brett used money he received as a gift for high school graduation to purchase $\$ 4,000$ worth of shares of stock. After he graduated from college, he needed money to buy a car, so he sold the stock for $\$ 2,433$. What was his capital gain or loss?

## EXAMPLE 2

Five years ago, Jessica bought 300 shares of a cosmetics company's stock for $\$ 34.87$ per share. Yesterday she sold all of the shares for $\$ 41$ per share. What was her capital gain?

SOLUTION Multiply to find the purchase price of all 300 shares. Multiply to find the selling price of all 300 shares. Subtract to find the capital gain.

Multiply purchase price by $300 . \quad 34.87 \times 300=10,461$
Multiply selling price by 300. $41 \times 300=12,300$
Subtract.
$12,300-10,461=1,839$
Jessica's gross capital gain was \$1,839.

## CHECK YOUR UNDERSTANDING

Kelvin bought 125 shares of stock for $\$ 68.24$ per share. He sold them nine months later for $\$ 85.89$ per share. What was his capital gain?

## EXTEND YOUR UNDERSTANDING

Three years ago, Maxine bought 450 shares of stock for $x$ dollars per share. She sold them last week for $y$ dollars per share. Express her capital gain algebraically in terms of $x$ and $y$.

## EXAMPLE 3

: Randy paid \$3,450 for shares of a corporation that manufactured cell phones. He sold it for $\$ 6,100$. Express his capital gain as a percent of the original purchase price. Round to the nearest tenth of a percent.
SOLUTION Find the amount of capital gain from the sale.
Capital gain $=$ Selling price - Purchase price
Substitute values. $\quad$ Capital gain $=6,100-3,450=2,650$
Think of $\$ 2,650$ as part of a whole. The whole is $\$ 3,450$. You need to express "what percent of 3,450 is 2,650 " as an equation. Let $x$ represent the percent increase, expressed as a decimal.
Write the equation.

$$
\begin{aligned}
(x)(3,450) & =2,650 \\
x & =\frac{2,650}{3,450} \\
x & \approx 0.7681
\end{aligned}
$$

Calculate.
Randy earned a 76.8\% capital gain on his investment.

## CHECK YOUR UNDERSTANDING

Allison bought shares in Citigroup Corporation in early 2007 for $\$ 55$ per share. She sold them later that year for $\$ 35$ per share. Express her loss as a percent of the purchase price. Round to the nearest percent.

## EXAMPLE 4

: Andy paid $w$ dollars for shares of a corporation that manufactured cell phones. He sold it for $y$ dollars. Express his capital gain as a percent of the original purchase price. Round to the nearest tenth of a percent.
SOLUTION Find the capital gain using variables.
Capital gain $=$ Selling price - Purchase price
Substitute values. $\quad$ Capital gain $=y-w$
Think of $y-w$ as part of a whole. The whole is $w$. Express "what percent of $w$ is $y-w^{\prime \prime}$ as an equation. Let $x$ represent the percent increase, expressed as a decimal.
Write the equation. Solve for $x$.

$$
\begin{aligned}
(x)(w) & =y-w \\
x & =\frac{y-w}{w}
\end{aligned}
$$

Divide each side of equation by $w$.
Andy earned a capital gain of $100 \frac{(y-w)}{w}$ percent on his investment.

## CHECK YOUR UNDERSTANDING

Linda bought $\$ 800$ of stock in a garden equipment corporation. The selling price is $x$ dollars. Express the percent increase of Linda's potential capital gain algebraically.

## Applications

When somebody buys a stock it's because they think it's going to
go up and the person who sold it to them thinks it's going to go
down. Somebody's wrong.
George Ross, Television actor

1. Is it always true that someone sells a stock because they think it is going to go down in price? How do those words apply to what you've learned in this lesson?
2. Zach bought 200 shares of Goshen stock years ago for $\$ 21.35$ per share. He sold all 200 shares today for $\$ 43$ per share. What was his gross capital gain?
3. Mitchell bought 600 shares of Centerco two years ago for $\$ 34.50$ per share. He sold them yesterday for $\$ 38.64$ per share.
a. What was the percent increase in the price per share?
b. What was the total purchase price for the 600 shares?
c. What was the total selling price for the 600 shares?
d. What was the percent capital gain for the 600 shares?
e. How does the percent increase in the price of one share compare to the percent capital gain for all 600 shares?
4. Tori bought $x$ shares of Mattel stock for $m$ dollars per share. She sold all of the shares months later for $y$ dollars per share. Express her capital gain or loss algebraically.
5. Ramon bought $x$ shares of Xerox stock for a total of $\$ 40,000$. Express the price he paid per share algebraically.
6. In 2004, Joe bought 200 shares in the Nikon corporation for $\$ 12.25$ per share. In 2007 he sold the shares for $\$ 31.27$ each.
a. What was Joe's capital gain?
b. Express Joe's capital gain as a percent, rounded to the nearest percent.
7. General Motors stock fell from $\$ 32$ per share in 2006 to $\$ 20$ per share during 2008.
a. If you bought and then sold 300 shares at these prices, what was your loss?
b. Express your loss as a percent of the purchase price. Round to the nearest tenth of a percent.
8. Elliott purchased shares of Microsoft in 2008 for $\$ 28$ per share. He plans to sell them as soon as the price rises $20 \%$. At what price will he sell his shares?
9. Maria purchased 1,000 shares of stock for $\$ 35.50$ per share in 2003. She sold them in 2007 for $\$ 55.10$ per share. Express her capital gain as a percent, rounded to the nearest tenth of a percent.
10. Austin purchased shares of stock for $x$ dollars in 2004. He sold them in 2010 for $y$ dollars per share.
a. Express his capital gain algebraically.
b. Express his capital gain as a percent of the purchase price.
11. During 2003, a share of stock in the Coca-Cola Company sold for $\$ 39$. During 2008, the price hit $\$ 56$ per share. Express the increase in price as a percent of the price in 2003. Round to the nearest tenth of a percent.
12. Alexa purchased 700 shares of Campagna Corporation stock for $x$ dollars per share in 2005. She sold them in 2010 for $y$ dollars per share, where $y<x$.
a. Did Alexa have a gross capital gain or a gross capital loss? Explain.
b. Alexa used the formula $\frac{700 y-700 x}{700 x}$ to compute the percent of the loss. Her husband Tom used the formula $\frac{y-x}{x}$ to compute the percent of the loss. She told him he was incorrect because he didn't take into account that she bought 700 shares. He says that his formula is correct, and so is hers. Who is correct, Alexa or Tom? Explain.
13. Zeke bought $g$ shares of stock for $w$ dollars per share. His broker called him and told him to sell the shares when they earn a $40 \%$ capital gain.
a. Express the total purchase price of all the shares algebraically.
b. Express the capital gain algebraically.
c. Zeke decides to sell his shares. Express the total selling price of all the shares algebraically.
14. Jake bought $d$ shares of stock for $x$ dollars per share years ago. His stock rose in price and eventually hit a price that would earn him a $140 \%$ capital gain. He decided to sell half of his $d$ shares.
a. Represent half of the $d$ shares algebraically.
b. Represent the capital gain earned on each of the shares that were sold algebraically.
c. Represent the capital gain earned on all of the shares that were sold algebraically.
d. Represent the total value of the shares that were sold algebraically.
e. Jake keeps the remaining half of the shares for several more years. The company goes bankrupt and those shares become worthless. Jake had a large gain on the shares he sold earlier-and took a loss on the shares that became worthless. Did investing in the $d$ shares result in a capital gain or loss for Jake? Explain using the algebraic expressions you created in parts a-d.
15. Ahmad sold 125 shares of stock for $x$ dollars that he had purchased for $\$ 32.75$ per share.
a. How much did he originally pay for the shares of stock?
b. Write an inequality that represents an amount such that Ahmad made money from the sale of the stocks.
c. Suppose Ahmad lost money on the stocks. Write an inequality that represents an amount such that Ahmad lost no more than $\$ 1,000$ from the sale of the stocks.

## 1-7 Stock Transaction Fees

## Objectives

- Compute the fees involved in buying and selling stocks.
- Become familiar with the basic vocabulary of stock trading.


## Key Terms

- stockbroker
- at the market
- broker fee
- limit order
- commission
- discount broker
- net proceeds


## How do you buy and sell stock?

You don't buy stock at a store. Shares of stock can only be purchased through a licensed stocklbroker. If you decided to sell your shares, you couldn't bring them to school and sell them to someone in the cafeteria. You also cannot walk into a stock exchange to sell your shares. Only stockbrokers buy and sell stocks. They also give advice to investors. For their services, stockbrokers charge a broker fee. The broker fee can be a flat fee, which does not depend on the value of the transaction, or a commission, which does depend on the value of the
 transaction. A commission is a percentage of the value of the stock trade.

Some people make their own investment decisions. They read the financial newspapers and websites to learn about new developments in the stock market. They still must buy and sell through brokers, but they may decide to use a discount broker. Discount brokers charge low fees. They do not give investment advice. They only make stock transactions. Discount brokers are available online, by phone, and in person. An online trading account is convenient because the investor can access it
24 hours a day.
If you buy or sell at the market, you are instructing your broker to get the best available price. You can also place a limitt order, which specifies the price you want to pay. If you put in a limit order to buy a stock only for a specific price, your broker will not make a purchase for any price higher than the price specified.

The fees you pay brokers when buying or selling stock affect the amount you gain or lose on the trade. Your net proceedls represent the amount of money you make after broker fees are subtracted. Make sure you are aware of the broker fees whenever you make a stock trade.

## Skills and Strategies

To compute the actual gain or loss for a given stock trade, you need to include the broker fees in your calculations.

## EXAMPLE 1

: Lee made two trades through his online discount broker, We-Trade. We-Trade charges a fee of $\$ 12$ per trade. Lee's first purchase was for $\$ 3,456$ and his second purchase, later in the day, was for $\$ 2,000$. How much did he spend on the day's purchases, including broker fees?
SOLUTION Lee made two trades. He paid two broker fees.
Fee $\times$ Number of trades
$(2)(\$ 12)=24$

Lee paid $\$ 24$ in broker fees. Next, find the sum of his purchases.
Add amount of both trades. $3,456+2,000=5,456$
The purchase price of the stock was $\$ 5,456$. Find the total spent.
Fee + Total purchase price $\quad 5,456+24=5,480$
Lee spent $\$ 5,480$ on the trades using his online discount broker.

## CHECK YOUR UNDERSTANDING

Garret made two trades in one day with his discount broker that charges $\$ 7$ per trade. Garret's first purchase was for $\$ 1,790$ and his second purchase was for $\$ 8,456$. How much did he spend including broker fees?

## EXAMPLE 2

- Adriana purchased \$7,000
worth of stock from a broker at Tenser Brokerage. The current value of Adriana's portfolio is $\$ 11,567$. What broker fee must she pay?

| Tenser Brokerage Fee <br> Schedule | Online <br> Trades |
| :--- | :--- |
| Portfolio value less | $\$ 15$ per <br> than $\$ 250,000$ |
| trade |  |
| Portfolio value greater |  |
| than \$250,000 | $\$ 12$ per <br> trade |


| Automated |
| :--- | :--- |
| Telephone Trades |$\quad$| Trades Using a <br> Broker |
| :---: |
| Online fee plus <br> $\$ 9.50$ |
| Online fee plus <br> $\$ 9.50$ |
| 0.5\% commission <br> plus online fee |
| $0.4 \%$ commission <br> plus online fee |

SOLUTION Adriana's fees are in the first row because her portfolio is under $\$ 250,000$. She is using a broker, so use the fees in the last column. First, multiply the percent expressed as an equivalent decimal by the amount of stock and add $\$ 15$.

$$
(0.005)(7,000)+15=50
$$

The total broker fee is $\$ 50$.

## CHECK YOUR UNDERSTANDING

Jared has a portfolio worth $\$ 500,000$. He made 10 telephone trades during the past year, buying and selling $\$ 50,000$ worth of stock.
What was his total broker fee for the year? Express his total broker fee algebraically if Jared had made $b$ automated telephone trades.

## EXAMPLE 3

Erin purchased $\$ 23,510$ worth of stock and paid her broker a $1 \%$ broker fee. She sold when the stock price increased to $\$ 27,300$, and used a discount broker who charged $\$ 21$ per trade. Compute her net proceeds.
SOLUTION Find the purchase cost.

$$
\begin{aligned}
\text { Purchase cost } & =\text { Cost of stock }+ \text { Broker fee } \\
& =23,510+(0.01)(23,510)=23,745.10
\end{aligned}
$$

When Erin sold the stock, the broker's fee was deducted from the sale price. Find Erin's sale proceeds.

$$
\begin{aligned}
\text { Sale proceeds } & =\text { Sale price of stock }- \text { Broker fee } \\
& =27,300-21=27,279
\end{aligned}
$$

The net proceeds is the difference between the purchase cost and the amount she received from her broker.

$$
\begin{aligned}
\text { Net proceeds } & =\text { Sale proceeds }- \text { Purchase cost } \\
& =27,279-23,745.10=3,533.90
\end{aligned}
$$

Erin's net proceeds were $\$ 3,533.90$.

## CHECK YOUR UNDERSTANDING

Yolanda purchased stock for \$7,000 and paid a 1.5\% broker fee. She sold it for $\$ 6,325$ and paid a $0.5 \%$ broker fee. Compute her net proceeds.

## EXAMPLE 4

Johan purchased stock six years ago for $x$ dollars and paid a $2 \%$ broker fee. He sold that stock yesterday for $y$ dollars and paid a discount broker $\$ 35$ for the sale. Express his net proceeds algebraically.
SOLUTION The purchase cost is the sum of the cost and the broker fee.

$$
\begin{aligned}
\text { Purchase cost } & =\text { Cost of stock }+ \text { Broker fee } \\
& =x+0.02 x
\end{aligned}
$$

When the stock was sold, the broker fee was $\$ 35$. The sale proceeds is the difference of the sale price and the broker fee.

> Sale proceeds = Sale price of stock - Broker fee

$$
=y-35
$$

The net proceeds is the difference between the purchase cost and the amount spent.

$$
\begin{aligned}
\text { Net proceeds } & =\text { Sale proceeds }- \text { Purchase cost } \\
& =(y-35)-(x+0.02 x)
\end{aligned}
$$

Simplify. The net proceeds are $y-35-1.02 x$.

## CHECK YOUR UNDERSTANDING

Rob purchased stock for $p$ dollars and paid a flat $\$ 40$ broker fee. Rob needed money for a home improvement so he sold it at a loss, for $h$ dollars, plus a $1 \%$ broker fee. Express his net proceeds algebraically.


1. How do those words apply to an investor? How do those words apply to a stockbroker?
2. Carlos does his online trading with Super Trade. Super Trade's rates are listed in the table below.

| Fee Schedule for Super <br> Trade Discount Broker | Online Trades | Automated Telephone <br> Trades | Telephone to a Live <br> Broker |
| :--- | :--- | :--- | :--- |
| less than 100 trades per <br> year | $\$ 17$ per trade | Online fee plus $\$ 11$ | $\frac{3}{4} \%$ commission plus <br> online fee |
| 100 or more trades per <br> year | $\$ 17$ per trade for the first <br> 100 shares, $\$ 14$ per trade <br> for trades over 100 | Online fee plus $\$ 11$ | $\frac{1}{2} \%$ commission plus <br> online fee |

a. If Carlos makes three dozen online trades in a year, what is the total of his broker fees?
b. What is the cost of 99 online trades?
c. What is the cost of 120 online trades?
d. If he makes $t$ online trades in a year, and $t>100$, express the total of his broker fees algebraically.
e. Suppose Carlos made $q$ online trades and $t$ automated telephone trades last year, where $q+t<100$. Express the cost of all the trades algebraically.
f. Suppose Carlos makes 20 trades in a year. If Carlos purchased $x$ shares of stock for $y$ dollars each using a phone call to a live broker, express the total broker fee algebraically.
3. The ticker shows trades of stock in Hewlett-Packard (HPQ), ExxonMobil (XOM), and Chevron (CVX).

```
HPQ 6K47.29 \nabla 0.23 XOM 3K92.67 ^ 0.08 CVX 9K100.38 \nabla 0.22
```

a. How many shares of Hewlett-Packard were sold?
b. What was the total value of all the HPQ shares sold?
c. Joan bought the shares at this price, and her broker charged her $1 \%$ commission. What was the total cost of her investment?
d. Reggie sold the shares of Exxon-Mobil shown in the above trade, and his broker charged him 1.5\% commission. How much money did the broker receive? Round to the nearest cent.
e. Lisa sold the shares of Chevron indicated above through her discount broker, who charges $\$ 28$ per transaction. How much money did Lisa receive from the above sale after the broker took his fee?
4. Taylor bought 200 shares of stock for $\$ 18.12$ per share last year. He paid his broker a flat fee of $\$ 30$. He sold the stock this morning for $\$ 21$ per share, and paid his broker $0.5 \%$ commission.
a. What were Taylor's net proceeds?
b. What was his capital gain?
5. Laura bought 55 shares of stock for $\$ 3.50$ per share last year. She paid her broker a $1 \%$ commission. She sold the stock this week for $\$ 2$ per share, and paid her broker a $\$ 10$ flat fee.
a. What were Laura's net proceeds? Round to the nearest cent.
b. What was her capital gain or loss?
6. Lenny bought $x$ shares of stock for $\$ y$ per share last month. He paid his broker a flat fee of $\$ 20$. He sold the stock this month for $\$ p$ per share, and paid his broker a $2 \%$ commission. Express Lenny's net proceeds algebraically.
7. Mackin Investing charges its customers a $1 \%$ commission. The Ross Group, a discount broker, charges $\$ 25$ per trade. For what amount of stock would both brokers charge the same commission?
8. Fierro Brothers, a discount broker, charges their customers a $\$ 19$ flat fee per trade. The Sondo Investment House charges a $2 \%$ commission. For what amount of stock would both brokers charge the same commission?
9. Darlene purchases $\$ 20,000$ worth of stock on her broker's advice and pays her broker a $1.5 \%$ broker fee. She sells her stock when it increases to $\$ 28,600$ two years later, and uses a discount broker who charges $\$ 21$ per trade. Compute Darlene's net proceeds after the broker fees are taken out.
10. Alex purchases $x$ dollars worth of stock on his broker's advice and pays his broker a $1 \%$ broker fee. The value of the shares falls to $y$ dollars years later, and Alex uses a broker who charges $1.25 \%$ commission to make the sale. Express his net proceeds algebraically.
11. Ron bought $x$ dollars worth of stock and paid a $y$ percent commission. Dave purchased $p$ dollars worth of stock and paid a $q$ percent commission, where $x>p$. Pick numbers for $x, y, p$, and $q$ such that Ron's commission is less than Dave's.
12. Debbie buys 400 shares of stock for $\$ 23$ per share, and pays a $1 \%$ commission. She sells them six years later for $\$ 23.25$ per share, and pays a $\$ 30$ flat fee. Are her net proceeds positive or negative? Explain.
13. Sal bought $x$ shares of a stock that sold for $\$ 23.50$ per share. He paid a $1 \%$ commission on the sale. The total cost of his investment, including the broker fee, was $\$ 3,560.25$. How many shares did Sal purchase?

## Stock Splits

## Key Terms

- stock split
- outstanding shares
- market capitalization or market cap
- traditional stock split
- reverse stock split
- penny stock
- fractional part of a share


## Objectives

- Calculate the post-split outstanding shares and share price for a traditional split.
- Calculate the post-split outstanding shares and share price for a reverse split.
- Calculate the fractional value amount that a shareholder receives after a split.
that the stock is worth more. This often happens to stocks known as penny stocks, whose value is less than $\$ 5$ per share. To increase the perceived value, the corporation may increase the price per share while at the same time decreasing the number of shares outstanding. This type of split is also in the form $a$ for $b$ where $a$ is less than $b$. For example, in a 1 -for- 2 split, the investor holding shares would now own one share for every two previously held. The price for that share would have doubled. The market capitalization remains the same.

The saying "perception is reality" holds true for the stock market. Although stock splits may not initially alter the value of shares held, the perception of change may lead to increases in sales and market prices.


Here you will learn how to interpret and calculate stock splits.

## EXAMPLE 1

: On December 4, John Deere Corporation (DE) instituted a 2-for-1 stock split. Before the split, the market share price was $\$ 87.68$ per share and the corporation had 1.2 billion shares outstanding. What was the presplit market cap for John Deere?

SOLUTION The market cap before the split is determined by multiplying the number of outstanding shares by the market price at that time.

Pre-split market cap $=$ Number of shares $\times$ Market price
$=1,200,000,000 \times 87.68$
$=105,216,000,000$
The pre-split market cap is $\$ 105,216,000,000$.

## CHECK YOUR UNDERSTANDING

A corporation has a market capitalization of $\$ 24,000,000,000$ with 250 M outstanding shares. Calculate the price per share.

## EXAMPLE 2

What was the post-split number of shares outstanding for John Deere?
SOLUTION Use a proportion to determine the number of outstanding shares available after the split. Let $x$ be the post-split outstanding shares.
$\begin{array}{ll}\frac{\text { Post-split }}{\text { Pre-split }} & \frac{2}{1}=\frac{x}{1.2} \\ \text { Cross multiply. } & x=2 \times 1.2\end{array}$
After the split, there will be 2.4 B shares outstanding.

## CHECK YOUR UNDERSTANDING

QualComm, Inc. instituted a 4 -for-1 split in November. After the split, Elena owned 12,800 shares. How many shares had she owned before the split?

## EXAMPLE 3

What was the post-split market price per share for John Deere in Example 1? How many shares are outstanding? Did the market cap change after the split?

SOLUTION This was a 2-for-1 stock split, so the new share price is $\frac{1}{2}$ the old share price.

$$
\frac{1}{2} \times 87.68=\$ 43.84
$$

In a 2 -for- 1 split the number of shares are doubled, so there are now

$$
2 \times 1.2=2.4 \mathrm{~B} \text { shares }
$$

The post-split market cap is $\$ 43.84 \times 2.4 \mathrm{~B}$ $=\$ 105,216,000,000$, which is the same as it was before.

## CHECK YOUR UNDERSTANDING

In October, Johnson Controls, Inc instituted a 3-for-1 split. After the split, the price of one share was $\$ 39.24$. What was the pre-split price per share?

## Post-Split Market Price and Number of Outstanding Shares

In general, in any $a$-for- $b$ split, you can apply the following formulas.
Post-split number of shares $=\frac{a}{b} \times$ Pre-split number of shares Post-split share price $=\frac{b}{a} \times$ Pre-split share price

## EXAMPLE 4

: On October 15, Palm, Inc. instituted a 1-for-20 reverse stock split. Before the split, the market share price was $\$ 0.64$ and there were $580,000,000$ shares. What was the post-split share price and number of shares?
SOLUTION Write the 1 -for- 20 reverse stock split as the ratio $\frac{1}{20}$.
Post-split number of shares $=\frac{a}{b} \times$ Pre-split number of shares

$$
=\frac{1}{20} \times 580,000,000=29,000,000
$$

Post-split share price $=\frac{b}{a} \times$ Pre-split share price

$$
=\frac{20}{1} \times 0.64=12.80
$$

After the split, there were 29 M shares outstanding with each share having a value of $\$ 12.80$. Notice that the pre-split market cap, $580 \mathrm{M} \times \$ 0.64$, and the post-split market cap, $29 \mathrm{M} \times \$ 12.80$, both equal $\$ 371,200,000$.

## CHECK YOUR UNDERSTANDING

A major drugstore chain whose stocks are traded on the New York Stock Exchange was considering a 2 -for- 5 reverse split. If the pre-split market cap was 1.71 B , what would the post-split market cap be?

## EXTEND YOUR UNDERSTAND\|NG

Suppose that before a stock split, a share was selling for $\$ 2.35$. After the stock split, the price was $\$ 7.05$ per share. What was the stock-split ratio?

## Fractional Part of a Share

The previous examples had shares that could be split into whole-number amounts. In reality, this may not be the case. Often the split would create a frractionall part of a share. In other words, there is less than one share remaining. When this happens, the corporation buys the fractional share at the current market price.

## EXAMPLE 5

Steve owned 942 shares of Graham Corporation. On January 3, a 5 -for-4 split was announced. The stock was selling at $\$ 56$ per share before the split. How was Steve financially affected by the split?
SOLUTION Write the split as a ratio. Use the pre-split information to find the post-split values.

$$
\begin{aligned}
\text { Post-split number of shares } & =\frac{a}{b} \times \text { Pre-split number of shares } \\
& =\frac{5}{4} \times 942=1,177.5 \\
\text { Post-split share price } & =\frac{b}{a} \times \text { Pre-split share price } \\
& =\frac{4}{5} \times 56=44.80
\end{aligned}
$$

Fractional shares are not traded, so the corporation paid him the market value of 0.5 shares.
Fractional part $\times$ Market price $\quad 0.5 \times 44.80=22.40$
Steve received $\$ 22.40$ in cash and 1,177 shares worth $\$ 44.80$ each.

## CHECK YOUR UNDERSTANDING

Gabriella owned 1,045 shares of Hollow Corporation at a price of $\$ 62.79$. The stock split 3 -for-2. How was Gabriella financially affected by the split?


Perception is strong and sight is weak. In strategy, it is important
to see distant things as if they were close and to take a distanced
view of close things.
Miyamoto Musashi, Japanese Samaurai, Artist, and Strategist

1. Why should investors be cautious when a split occurs? How might those words apply to what you have learned?
2. In February, Robbins and Myers, Inc. executed a 2 -for- 1 split. Janine had 470 shares before the split. Each share was worth $\$ 69.48$.
a. How many shares did she hold after the split?
b. What was the post-split price per share?
c. Show that the split was a monetary non-event for Janine.
3. On June 5, CIGNA instituted a 3 -for- 1 stock split. Before the split, CIGNA had 200 million shares with a price of $\$ 168$ per share.
a. How many shares were outstanding after the split?
b. What was the post-split price per share?
c. Show that this split was a monetary non-event for the corporation.
4. Vilma owns 750 shares of Aeropostale. On August 22, the corporation instituted a 3 -for- 2 stock split. Before the split, each share was worth $\$ 34.89$.
a. How many shares did Vilma hold after the split?
b. What was the post-price per share after the split?
c. Show that the split was a monetary non-event for Vilma.
5. Mike owns 2,400 shares of JDS Uniphase Corp. The company instituted a 1 -for-8 reverse stock split on October 17. The pre-split market price per share was $\$ 2.13$.
a. How many shares did Mike hold after the split?
b. What was the post-split price per share?
c. Show that the split was a monetary non-event for Mike.
6. Versant Corporation executed a 1-for-10 reverse split on

August 22. At the time, the corporation had $35,608,800$ shares
outstanding and the pre-split price per share was $\$ 0.41$.
a. How many shares were outstanding after the split?
b. What was the post-price per share after the split?
c. Show that this split was a monetary non-event for the corporation.
7. Kristy owns 200 shares of Nortel stock. On November 30 the company instituted a 1 -for-10 reverse split. The pre-split price per share was $\$ 2.15$. The number of shares outstanding before the split was 4.34 B .
a. How many shares did Kristy hold after the split?
b. What was the post-split price per share?
c. What was the post-split number of outstanding shares?
d. What was the post-split market cap?

Jon noticed that most traditional splits are in the form $\boldsymbol{x}$-for-1. He says that in those cases, all you need do is multiply the number of shares held by $\boldsymbol{x}$ and divide the price per share by $\boldsymbol{x}$ to get the post-split numbers. Answer Exercises 8-9 based on Jon's method.
8. Verify that Jon's method works to determine the post-split price and shares outstanding for Hansen Natural Corporation which executed a 4 -for- 1 split on July 10 with $22,676,800$ outstanding shares and a market price of $\$ 203.80$ per share before the split.
9. Jon also noticed that every traditional split ratio can be written in the form $x$-for-1. Examine how the 3 -for- 2 traditional split can be expressed as 1.5 -for- 1 .

$$
\frac{3}{2}=\frac{x}{1} \rightarrow 3=2 x \rightarrow x=1.5
$$

Express each of the following traditional split ratios as $x$-for- 1 .
a. 5-for-4
b. 6-for-5
c. 5-for-2
d. 8 -for- 5
10. Monarch Financial Holdings, Inc. executed a 6 -for- 5 traditional split on October 5. Before the split there were approximately $4,800,000$ shares outstanding, each at a share price of $\$ 18.00$.
a. Use the method outlined in Examples 2 and 3 on pages 46 and 47 to determine the post-split share price and number of shares outstanding.
b. Compare the results from part a. with that obtained by using Jon's method. Jon's method says that 6 -for-5 is the same as 1.2-for-1.
11. On June 19 California Pizza Kitchen, Inc. instituted a 3 -for- 2 split. At that time Krista owned 205 shares of that stock. The price per share was $\$ 33.99$. After the split, Krista received a check for a fractional part of a share. What was the amount of that check?
12. On December 14, XTO Energy, Inc. executed a 5 -for- 4 split. At that time, Bill owned 325 shares of that stock. The price per share was $\$ 65.80$. After the split he received a check for a fractional part of a share. What was the amount of that check?

Use the following spreadsheet to answer Exercises 13-15. The split-ratio is entered in cells B2 and C2. For example, the ratio of 2 -for- 1 would be entered as a 2 in B 2 and a $1 \mathrm{in} \mathrm{C2}$. The number of pre-split shares is entered in B3 and the pre-split price is entered in B4.
13. Write the spreadsheet formula that will calculate the post-split number of outstanding shares in C3.
14. Write the spreadsheet formula that will calculate the post-split price per share in C4.
15. Write the pre-split market cap formula in cell B9 and the post-split market cap formula in C9.

|  | A | B | C |
| :---: | :---: | :---: | :---: |
| 1 |  | Pre-split | Post-split |
| 2 | Split ratio | 2 | 1 |
| 3 | Outstanding shares |  |  |
| 4 | Price per share |  |  |
| 5 | Market cap |  |  |

## Dividend Income

## 1-9

## Key Terms

- dividend
- dividend income
- income stock
- yield
- growth stock
- preferred stock
- common stock
- corporate bond
- face value
- matures


## IF SHAREHOLDERS OWN A CORPORATION,

 ARE THEY ENTITLED TO SOME OF THE PROFITS?If you buy a stock and watch its price rise, it's exciting, but your profit is only realized when you actually sell it. Keep in mind that capital gains and net proceeds cannot be computed and are not assured until the stock is actually sold. However, your stock portfolio can earn income before you sell your shares. Remember, a shareholder is an owner of a corporation. As owners, shareholders are entitled to their portions of the corporation's profit. Profit split among shareholders is called a dividend. Money received from dividends is dlividendl income. Dividends are usually paid annually or quarterly. The board of directors of the corporation sets the dividend for one share of stock. For major public corporations this can be found under a column headed "Div" in newspaper or online stock tables. Your total dividend depends on the number of shares you own. Some corporations do not pay a dividend because the profit is being used to improve or grow the corporation. Some corporations do not pay a dividend because they have no profit. They are operating at a loss. Stocks that pay dividends are called income stocks, because they provide their owners with income.

Some people buy income stocks which pay dividends for the additional income. The yield of a stock is the percentage value of the dividend, compared to the current price per share. Investors use the yield to compare their dividend income to the interest they could have made if they put the money in the bank instead of buying the stock. Other investors are not concerned with dividend income. Instead, they want to buy low and sell high. Stocks that are bought for this reason are called growth stocks. A stock can be both an income and a growth stock.

Stocks are also classified as preferred stock or common stock. Preferred stockholders receive their dividends before common stockholders do, and they usually receive a set dividend which does not frequently change. Common stockholders receive dividends only when the board of directors elects to issue these dividends. Additionally, if a company goes out of business, preferred stockholders are entitled to assets and earnings of the company, ahead of common stockholders.

## Objectives

- Understand the concept of shareowners splitting the profit of the corporation they own.
- Compute dividend income.
- Compute the yield for a given stock.
- Compute the interest earned on corporate bonds.

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Dividend payments are mailed to shareholders or electronically transferred to their accounts. Dividend payments can range in value from a few cents to thousands of dollars, because they depend on how much the dividend is and how many shares are owned. Remember that dividends are not guaranteed and can be cut or eliminated if the company decides they need the money. Although, most companies do not like to cut dividends and disappoint shareholders.

## Skills and Strategies

If your stock pays a dividend, you want to make sure the amount you are receiving is correct. You also want to be aware of how dividend income compares to the bank interest you could have made if you decided to put the money in the bank instead of buying the stock.

## EXAMPLE 1

Roberta is considering purchasing a common stock that pays an annual dividend of $\$ 2.13$ per share. If she purchases 700 shares for $\$ 45.16$ per share, what would her annual income be from dividends?

SOLUTION The price paid per share is not needed to compute the annual dividend. To find the annual income from dividends, multiply the number of shares by the annual dividend per share.
Income from dividends $=$ Number of shares $\times$ Dividend per share

$$
=700 \times 2.13=1,491
$$

The annual income from dividends is $\$ 1,491$.

## CHECK YOUR UNDERSTANDING

Jacques purchased $x$ shares of a corporation that pays a $y$ dollar annual dividend. What is his annual dividend income, expressed algebraically?

## EXAMPLE 2

: Elyse owns 2,000 shares of a corporation that pays a quarterly dividend of $\$ 0.51$ per share. How much should she expect to receive in a year?
SOLUTION First, compute her quarterly dividend by multiplying the total number of shares by the quarterly dividend per share.
Income from dividends $=$ Number of shares $\times$ Dividend per share

$$
=2,000 \times 0.51=1,020
$$

To find the amount she should expect to receive in a year, multiply by 4.

$$
1,020 \times 4=4,080
$$

Elyse should receive $\$ 4,080$ in a year.

## CHECK YOUR UNDERSTANDING

Monique owns $x$ shares of stock. The quarterly dividend per share is $y$ dollars. Express Monique's annual dividend amount algebraically.

## Yield

To find the yield of a stock, write the ratio of the annual dividend per share to the current price of the stock per share and convert to a percent. A yield can change even when a dividend amount does not because the price of the stock changes frequently.

## EXAMPLE 3

- Kristen owns common stock in Max's Toy Den. The annual dividend is $\$ 1.40$. The current price is $\$ 57.40$ per share. What is the yield of the stock to the nearest tenth of a percent?
SOLUTION Write the yield as a fraction. Then convert the fraction to a decimal. Finally write the decimal as a percent.

$$
\begin{aligned}
\text { Yield } & =\frac{\text { Annual dividend per share }}{\text { Current price of one share }} \\
& =\frac{1.40}{57.40} \approx 0.0243902, \text { or } 2.4390 \%
\end{aligned}
$$

The yield is about $2.4 \%$.

## CHECK YOUR UNDERSTANDING

You bought $x$ shares of a stock for $\$ y$ per share. The annual dividend per share is $\$ d$. Express the percent yield algebraically.

## EXAMPLE 4

: One share of BeepCo preferred stock pays an annual dividend of \$1.20.

- Today BeepCo closed at $\$ 34.50$ with a net change of $-\$ 0.50$. What was the stock's yield at yesterday's closing price?
SOLUTION Use today's close and the net change to find yesterday's close.
Today's close + Opposite of net change $34.50-(-0.50)=35$
Yesterday's close was $\$ 35.00$.

$$
\begin{aligned}
\text { Yield } & =\frac{1.20}{35} \\
& \approx 0.03429, \text { or } 3.4 \%
\end{aligned}
$$

At yesterday's close, the yield was about 3.4\%.

## CHECK YOUR UNDERSTANDING

One share of Skroy Corporation stock pays an annual dividend of $\$ 1.55$. Today Skroy closed at $x$ dollars with a net change of +0.40 . Express the yield at yesterday's close algebraically.

## EXAMPLE 5

A stock paid an annual dividend of $\$ 2.14$. The stock split 2-for-1. What is the annual dividend after the split?
SOLUTION After a 2 -for-1 split, there are twice as many shares outstanding, so divide the dividend by $2: 2.14 \div 2=1.07$. The new annual dividend per share is $\$ 1.07$.

## CHECK YOUR UNDERSTANDING

A corporation was paying a $\$ 2.10$ annual dividend. The stock underwent a 3 -for- 2 split. What is the new annual dividend per share?

## Corporate Bonds

Buying stock has risk and rewards. If you do not want to take a significant risk, you can invest in corporate bonds. A corporate bondl is a loan to a corporation. The corporation agrees to pay the bondholder back with interest, much like a bank does to customer with money on deposit. The interest is usually paid annually or semiannually. Usually, corporate bonds are for $\$ 1,000$ or $\$ 5,000$. This amount is the face vallue and is the amount paid when the bond matures. Bondholders do not share in any profits, and they do not own part of the corporation. Investors that buy bonds enjoy less risk and have less potential rewards.

The maturity date of a bond is a date in the future when the principal invested will be repaid to the investor The time to maturity can be a short period or as long as 30 years. Upon maturity, an investor will receive the amount originally invested back from the corporation. Bonds that take longer to mature generally pay a higher interest rate.

## EXAMPLE 6

Adam bought a $\$ 1,000$ corporate bond in the Labate Corporation. The bond pays $5.7 \%$ interest per year. How much does Adam receive in interest each year from this bond?

SOLUTION To find the annual interest, first convert the percent to an equivalent decimal.

$$
5.7 \%=0.057
$$

Then, multiply the interest expressed as a decimal by the face value.
Multiply interest by $1,000 \quad 0.057 \times 1,000=57$
Adam receives $\$ 57$ in annual interest.

## CHECK YOUR UNDERSTANDING

If Adam holds the bond from Example 6 for 11 years, how much will he receive in total interest?

## Applications

I believe non-dividend stocks aren't much more than baseball
cards. They are worth what you can convince someone to pay for them.

Mark Guban, Billionaire businessman

1. Based on what you learned about dividends, why are non-dividend stocks compared to baseball cards?
2. Years ago, Home Depot had an annual dividend of $\$ 0.90$. If you owned 4,000 shares of Home Depot, how much did you receive annually in dividends?
3. Barnes and Noble had a $\$ 1.00$ annual dividend during 2008. If you owned 500 shares of Barnes and Noble, how much did you receive on a quarterly dividend check?
4. If you own $r$ shares of a stock with an annual dividend of $p$ dollars, express the amount of your quarterly dividends algebraically.
5. The quarterly dividend for Tiffany, a jewelry company, was $\$ 0.17$ during the second quarter of 2008. What was the annual dividend for 2,000 shares?
6. Mike owned 3,000 shares of Merck Corporation and received a quarterly dividend check for $\$ 1,140$. What was the annual dividend for one share of Merck?
7. Jean owned $x$ shares of a corporation and received a quarterly dividend check for $y$ dollars. Express the annual dividend for one share algebraically.
8. The Walt Disney Company paid a $\$ 0.35$ annual dividend on a day it closed at a price of $\$ 33.86$ per share.
a. What was the annual dividend for 500 shares?
b. What was the quarterly dividend for 500 shares?
c. Express the yield as a fraction.
d. What was the yield to the nearest tenth of a percent?
9. You own $K$ shares of a stock that is selling for $x$ dollars per share. The quarterly dividend is $y$ dollars per share.
a. Express the annual dividend for one share algebraically.
b. Express the annual dividend for all $k$ shares algebraically.
c. Express the yield as an algebraic fraction.
10. The spreadsheet on the right can be used to compute the yield. Write the formula that can be used to compute the yield in cell C2.
11. The Black Oyster Corporation is going out of business. All of the corporate assets are being sold. The money raised will be split by the stockholders. Which stockholders, the common or preferred, receive money first?

|  | A | B | C |
| :---: | :---: | :---: | :---: |
|  | Price per <br> Share | Annual <br> Dividend | Yield |
| 2 | 37.12 | 1.51 |  |
| 3 | 44.55 | 1.77 |  |
| 4 | 65.29 | 2.01 |  |
| 5 | 14.35 | 0.48 |  |


| Name | Last <br> Price | Dividend |
| :--- | ---: | :---: |
| 3M Co | 76.90 | 2.00 |
| Alcoa, Inc | 41.57 | 0.68 |
| American Express Co | 46.15 | 0.72 |
| American International Group, Inc | 34.91 | 0.80 |
| AT\&T, Inc | 39.51 | 1.60 |
| Bank of America Corp | 33.87 | 2.56 |
| Boeing Co | 82.13 | 1.60 |
| Caterpillar, Inc. | 83.19 | 1.44 |
| Chevron Corp | 100.42 | 2.60 |
| Citigroup, Inc. | 57.60 | 1.28 |
| Coca-Cola Co/The | 1.52 |  |
| El Du Pont de Nemours \& Co | 47.63 | 1.64 |
| Exxon Mobil Corp | 90.43 | 1.60 |

## For Exercises 12-15, round answers to the nearest tenth of a percent.

12. The table gives the last price and the annual dividend for 15 corporations. Compute the yield for each corporation.
13. The Revreg Corporation pays an annual dividend of $\$ 1.60$ per share. On Friday it closed at $\$ 44$ per share with a net change of +0.35 . The dividend did not change.
a. What was the yield on Friday?
b. At what price did Revreg close on Thursday?
c. What was the yield at Thursday's close?
d. Thursday's net change was +1.22 .

At what price did Reverg close on Wednesday?
e. If the dividend was $\$ 1.60$ on Wednesday, what was the yield at Wednesday's close?
f. Look at the yields for Wednesday, Thursday, and Friday. They are decreasing. Explain why this decrease is not "bad news" to the investor who owns stock in Revreg.
14. The Zeescore Corporation pays an annual dividend of $\$ 2$ per share.

On Wednesday it closed at $\$ 61$ per share with a net change of -0.85 .
The dividend remained at $\$ 2$ for a year.
a. What was the yield on Wednesday?
b. At what price did Zeescore close on Tuesday?
c. What was the yield on Tuesday?
d. Tuesday's net change was -1.96 . At what price did Zeescore close on Monday?
e. What was Monday's yield?
f. Look at the yields for Monday, Tuesday, and Wednesday. They are increasing. Explain why this increase is not "good news" to the investor who owns stock in Zeescore.
15. Sascha owns stock in Lewis Corp and she bought a $\$ 1,000$ corporate bond. The bond pays $6.34 \%$ annual interest.
a. How much will Sascha receive in annual interest?
b. How much will Sascha receive in interest if she holds the bond for 14 years?
c. Sascha's stock is worth $\$ 46$ per share, and it pays a $\$ 2$ annual dividend. What is the yield?
d. Which is higher, the yield on the stock or the interest rate on the bond?
e. How much does Lewis Corp. pay to Sascha when the bond matures?
16. Stock in Happy's Burger Chain was selling for $\$ 54.24$ per share, and it was paying a $\$ 2.46$ annual dividend. It underwent a 3 -for- 1 split.
a. What was the new price of one share after the split?
b. If you owned 200 shares before the split, how many shares did you own after the split?
c. Following the same pattern, what was the annual dividend per share after the split?

## Assessment

## You Write the Story!!

## Real Numbers

Examine the graph below. Write a short newspaper-type article, using facts obtained online or at the library, centered around this graph. You can find an electronic copy of the graph at www.cengage.com/ school/math/financialalgebra. Copy and paste it into your article.


1. Choose a corporation that you are interested in following. Use the newspaper or Internet to find the daily low, high, close, and volume of your stock for the next three weeks. Set up a graph to record these prices and the volume. Discuss the trends for the three-week period. Check the corporation's website for major news about the corporation. Discuss the trend over the three-weeks and include any major corporate news that might have affected the trend.
2. Discuss stocks with your parents or guardians. Find out if they own any stocks currently, or ever did during their lives. If you earn money on your own, discuss with them the possibility of purchasing shares of stock for a corporation you are interested in following.
3. Survey your classmates and compile a list of questions your class has about stocks. Compile a list of the top five stocks they are interested in. Call a local stockbroker and request an appointment for a short meeting. Interview the broker. Ask the broker why these stocks may or may not be a good investment. Report your findings.
4. Visit a local bank and ask to speak to one of the representatives about United States Savings Bonds. Find out about the forms necessary to purchase a bond, the interest it pays, and how long the bonds take to reach their face value. Prepare a report and present your findings to the class.
5. Contact a local stockbroker. Talk to your teacher about setting up a class session featuring the stockbroker as a guest speaker. During the broker's presentation, conduct a question-and-answer session.
6. Contact the New York Stock Exchange by mail or through its website. Request a list of publications that the Exchange offers.
7. Use the library or Internet to research a corporation. Prepare a poster board about the corporation. Include how and when the corporation was founded, where it got its name, major developments in its history, and why you may or may not want to invest in this company.
8. Work with a small group of classmates to select 5 to 10 stocks that will form a stock portfolio. Set up an online portfolio using any financial website such as yahoo.com or nyt.com with an initial investment of $\$ 10,000$. Track the gains and losses of your entire portfolio for a month. Compare your total profit or loss with that of other groups.

GOOGLE.COM® ${ }^{\circledR}$ is derived from the number googol which is a 1 with 100 zeros following it. This is equivalent to $10^{100}$. The change in spelling (but not pronunciation) still elicits the feel of something very large. How large is $10^{100}$ ? There isn't a googol of anything on the planet!

Given that 1,000,000 pennies stacked one on top of another reaches about one mile high, how high will 1 googol pennies reach?

To get an idea of the "power" of exponents, investigate a famous problem in math. Imagine your teacher asks you to work at school for all of June. You can choose to be paid in one of two ways.

- One payment of $\$ 5,000$, which you will receive on June 30 .
- On the first day you get paid 14 . On the second day you receive double that amount, which is $2 \Varangle$. On the third day you receive $4 \varnothing$, on the fourth day $8 ¢$, and so on. Each day you get paid twice the amount you were paid the day before.


## Draw a grid with six columns and five rows to represent the 30 days. Fill in the amount you are paid each day.

1. How much do you receive on June 14 ? June 27 ? June 30 ?
2. Another way to think of the payment on June 30 is 1 cent multiplied by 2 twenty-nine times. What is the product of 0.01 and $2^{29}$ ?
Think about how much 29 multiplications by 2 inflated the original 1 cent! Imagine raising 10 to the 100th power! The stock market deals in billions and sometimes trillions of dollars, but remember that 1 billion $=10^{9}$ and 1 trillion $=10^{12}$. Nothing close to a googol. And that's reality!

## Applications

1. Nick and Matt are the partners in a local health food store. They needed $\$ 73,000$ to start the business. They invested in the ratio $3: 7$, Nick to Matt.
a. How much money did each invest?
b. What percent of the business was owned by Matt? Round to the nearest tenth of a percent.
2. Tom purchased shares of DuPont for $\$ 47.65$ per share. He plans to sell the shares when the stock price rises $20 \%$. At what price will he sell his shares?
3. The top three shareholders in a certain corporation each own $s$ shares of a certain stock. The corporation's ownership is represented by a total of $x$ shares of stock. Express the percent of the corporation owned by the top three shareholders algebraically.
4. Marilyn purchased 2,000 shares of stock for $\$ 25.43$ per share. She sold them for $\$ 44.10$ per share. Express her capital gain to the nearest tenth of a percent.
5. A local hairdresser bought 450 shares of a cosmetics corporation for $\$ 33.50$ per share. He sold the shares for $\$ 39.01$ per share.
a. What was the percent increase in the price per share? Round to the nearest tenth of a percent.
b. What was the total purchase price for the 450 shares?
c. What was the total selling price for the 450 shares?
d. What was the percent capital gain for the 450 shares? Round to the nearest tenth of a percent.
6. Deanna purchased $\$ 24,000$ worth of stock and paid her broker a $1 \%$ broker fee. She sold the stock when it increased to $\$ 29,100$ three years later and used a discount broker who charged $\$ 35$ per trade. Compute her net proceeds after the broker fees were taken out.
7. The Bootle Corporation paid Leslie a quarterly dividend check for $\$ 828$. Leslie owns 450 shares of Bootle. What was the quarterly dividend for one share of Bootle?
8. Aaron owned $x$ shares of a corporation and received an annual dividend of $y$ dollars. Express the quarterly dividend for one share algebraically.
9. The Zyco Corporation pays an annual dividend of $\$ 2.10$ per share. On Tuesday it closed at $\$ 72$ per share with a net change of +0.95 . The dividend remained at $\$ 2.10$ for several months.
a. What was the yield on Tuesday? Round to the nearest tenth of a percent.
b. At what price did Zyco close on Monday?
c. What was the yield at Monday's close? Round to the nearest tenth of a percent.

Market Data, Close on June 20

| $\begin{gathered} \text { 52-week } \\ \text { High } \end{gathered}$ | 52-week Low | Symbol | Stock | Last | Change | Sales 100s | High | Low |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 143.25 | 73.25 | PCU | Southern Copper Corp. | 108.88 | 3.61 | 2643.7 | 110.68 | 105.68 |
| 42.97 | 32.95 | T | AT\&T, Inc. | 34.43 | -0.72 | 43386.8 | 35.59 | 34.41 |
| 131.82 | 42.24 | ESI | ITT Ed Services | 88.40 | 3.91 | 3429.5 | 90.71 | 82.06 |
| 50.48 | 36.01 | JPM | JPMorgan Chase \& Co. | 37.86 | -0.79 | 553772 | 39.19 | 36.95 |

11. Use the table above to answer the following questions.
a. What was the difference between the 52 -week high and the 52-week low for one share of AT\&T?
b. What was the difference between the day's high and low for one share of Southern Copper?
c. Which stock had a close that was furthest from the day's low?
d. Determine the close on June 19 for JPMorgan Chase.
e. How many shares of ITT were traded on June 20?
f. What was the percent net change from June 19 to June 20 for AT\&T? Round to the nearest hundredth of a percent.
g. Which stock had a day's high that was approximately $30 \%$ less than its 52-week high?
h. On June 19, there were $59,945,400$ shares of JPM traded. What was the difference in the number of shares traded from June 19 to June 20?
12. Use the stock bar chart to answer questions below.

a. What was the day's open on June 17 ?
b. What was the approximate difference between the day's high and low on June 18?
c. On what day was the close also the day's low?
d. Write the approximate volume for June 19.
13. Use the candlestick chart to answer the questions below.
a. What was the approximate low on June 20?

b. What was the approximate high on this date?
c. What was the difference between the opening price and the close?
d. What does the red candlestick color indicate?
14. Lea owns 800 shares of ABC, Incorporated. On April 6 the corporation instituted a 5 -for- 2 stock split. Before the split, each share was worth $\$ 42.60$.
b. What was the post-split price per share?
c. Show that the split was a monetary non-event for Lea.
15. Gene owns 1,200 shares of XYX Corporation. The company instituted a 1 -for-10 reverse stock split on November 7. The pre-split market price per share was $\$ 1.20$.
a. How many shares did Gene hold after the split?
b. What was the post-split price per share?
c. Show that the split was a monetary non-event for Gene.
16. Use the table of closing prices for Microsoft. Round answers to the nearest cent.
a. Determine the 3-day moving averages.
b. Determine the 10 -day moving averages.

Use the following stock market ticker to answer Exercises 17 and 18.

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GE 12.5K@26.13^1.13 F .67K@5.01\nabla0.38 C 3K@16.19^
    1.47 T1.6K@26.14\nabla1.08
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17. Nick bought some shares of Ford Motor Company (F).
a. How many shares did Nick buy?
b. How much did each share cost?
c. What was the value of Nick's trade?
18. Patrick sold his shares of AT\&T (T).
a. How many shares did he sell?
b. For how much did each share sell?
c. Based on Patrick's sale, what was the closing price of T

| Date | Close | 3-day <br> Averages | 10-day <br> Averages |
| :---: | :---: | :---: | :---: |
| 23-May | 28.05 |  |  |
| 27-May | 28.44 |  |  |
| 28-May | 28.18 |  |  |
| 29-May | 28.31 |  |  |
| 30-May | 28.32 |  |  |
| 2-Jun | 27.80 |  |  |
| 3-Jun | 27.31 |  |  |
| 4-Jun | 27.54 |  |  |
| 5-Jun | 28.30 |  |  |
| 6-Jun | 27.49 |  |  |
| 9-Jun | 27.71 |  |  |
| 10-Jun | 27.89 |  |  |
| 11-Jun | 27.12 |  |  |
| 12-Jun | 28.24 |  |  |
| 13-Jun | 29.07 |  |  |
| 16-Jun | 28.93 |  |  | on the previous trading day?

19. The stock in a real estate corporation was selling for $\$ 78$ per share with an annual dividend of $\$ 1.86$. It underwent a 3 -for- 2 split.
a. What was the value of one share of the stock after the split?
b. What was the annual dividend after the split?
20. A stock that was selling for $\$ x$ per share underwent a $y$-for- $p$ split. It was originally paying an annual dividend of $\$ d$ per share. Express the annual dividend after the split algebraically.
21. Suki purchased $\$ 9,600$ worth of stock and paid her broker a $1.75 \%$ broker fee. She had an immediate need for cash and was forced to sell the stock when it was worth $\$ 8,800$. She used a discount broker who charged $\$ 32.50$ per trade. Compute Suki's net loss after the broker fees were taken out.
